## Ammann, Bernd: Moduli spaces of Riemannian and Lorentzian manifolds (SR1 c)

The goal of the talk is to explain some unexpected correspondences between moduli spaces of Riemannian and Lorentzian manifolds. In the first part we describe joint research with

Klaus Kr\"oncke, Hartmut Wei\ss{} and Olaf M\"uller. Let \$M\$ be a compact spin manifold. We consider the moduli space of Riemannian metrics on \$M\$ carrying a (non-trivial) parallel spinor. They are Ricci-flat, and all known Ricci-flat compact Riemannian manifolds are -- up to a finite covering -- of this kind. We explain that any curve in the moduli space of Ricci-flat metrics with parallel spinors yields a Lorentzian metric with a parallel lightlike spinor on \$[a,b]\times M\times (-\epsilon,\epsilon) \$. Under some mild conditions loops in the moduli space of Ricci-flat metrics with parallel spinors yield a Lorentzian metric with a parallel lightlike ike spinor on \$\$^1\times M\times (-\epsilon,\epsilon)\$.

In the second part we explain recent work by my student J. Gl\"ockle which provides non-trivial homotopy groups in the space of intial data sets for Lorentzian manifolds satisfying the dominant energy condition strictly. In general relativity, the dominant energy condition expresses non-negative local mass distribution. For totally geodesic spacelike hypersurfaces \$M\$ it yields that \$M\$ has non-negative scalar curvature. We consider the space

 $\$ DEC:=\{(g,k)\mid \textrm{strict dominant energy condition}\}.\$ The pair \$(g,0)\$ is in \$DEC\$ iff \$g\$ is in \$\mathcal{R}^+(M)\$, the space of metrics on \$M\$ with positive scalar curvature. We describe a map from the suspension of \$\mathcal{R}^+(M)\$ to \$DEC\$ with the following property: if \$S^k\to \mathcal{R}^+(M)\$ represents a non-trivial homotopy class detected by an index, then we obtain a map \$S^{k+1}\to DEC\$ with "the same" index.