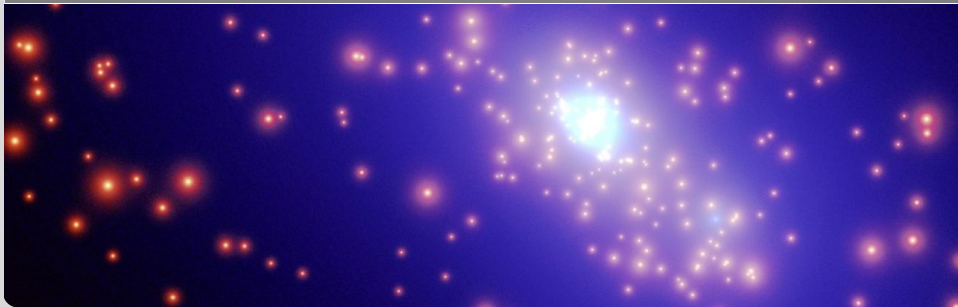


Constraints on Dark Matter Annihilation from the Rare $B_s \rightarrow \mu^+ \mu^-$ Decay in the MSSM with NMFV

Christoph Borschensky, Guillaume Chalons, Florian Domingo, Ulrich Nierste | May 14, 2012

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- 1 Introduction
 - Flavor Violation
 - Supersymmetry
 - Dark Matter
- 2 Effective Two Higgs Doublet Model
- 3 Chiral Enhancement
 - Chirally enhanced self energies
 - Scalar and Pseudoscalar Wilson Coefficients
- 4 Numerical Evaluation

The CKM matrix (1)

- Yukawa term for up-type quarks:

$$\mathcal{L}_Y \supset -Y_{fi}^u \bar{Q}_{fL} \tilde{\Phi} u_{iR}$$

with

$$Q_{fL} = \begin{pmatrix} u_{fL} \\ d_{fL} \end{pmatrix}, \quad \tilde{\Phi} = i\sigma^2 \Phi^*, \quad \Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

- Rotating the fields

$$Q_{fL} \rightarrow Q_{fL}^{\text{phys.}} = S_{jf}^* Q_{jL}$$

$$u_{iR} \rightarrow u_{iR}^{\text{phys.}} = U_{ki}^* u_{kR}$$

renders the Yukawa matrix diagonal in flavor space:

$$S_{jf}^* Y_{fi}^u U_{ik} = Y_j^{u(\text{diag.})} \delta_{jk}$$

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The CKM matrix (2)

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- Rotating the field

$$d_{iR} \rightarrow d_{iR}^{\text{phys.}} = D_{ki}^* d_{kR}$$

does not diagonalize Y_{fi}^d , since the rotation of Q_{fL} is already fixed:

$$S_{jf}^* Y_{fi}^d D_{ik} = (V Y^{d(\text{diag.})})_{jk}$$

with the so-called CKM matrix V containing off-diagonal entries.

⇒ Additionally rotate the down part of Q_{fL} with V to diagonalize down quark mass terms:

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■ *Charged currents (CC)*

- Standard Model (SM): W^\pm bosons
- Two Higgs Doublet Model (THDM): charged Higgs bosons H^\pm
- Minimal Supersymmetric Standard Model (MSSM): charginos $\tilde{\chi}_k^\pm$

■ *Flavor changing neutral currents (FCNC)*

- SM: Z^0 penguins, W^\pm boxes; **loop suppressed!**
- THDM: new flavor changing couplings (non-holomorphic); **on tree level!**
- MSSM: for a general flavor structure, squark mass matrices can induce flavor mixing on **tree level** as well

■ *Minimal flavor violation (MFV)*: Process proportional to a Yukawa matrix

■ *Non-minimal flavor violation (NMFV)*: General flavor structure (e.g. squark mass matrices in a general MSSM)

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- **SM** just an **effective low energy theory**; requires a **more comprehensive theory** at higher energies
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MSSM fields & particles

Supermultiplet	$SU(3)_C$	\times	$SU(2)_L$	\times	$U(1)_Y$	Particle content
$\hat{Q} \equiv \begin{pmatrix} \hat{u} \\ \hat{d} \end{pmatrix}$	3		2		$+\frac{1}{3}$	$\begin{pmatrix} u_L \\ d_L \end{pmatrix}, \begin{pmatrix} \tilde{u}_L \\ \tilde{d}_L \end{pmatrix}$
\hat{U}	3		1		$+\frac{4}{3}$	u_R, \tilde{u}_R
\hat{D}	3		1		$-\frac{2}{3}$	d_R, \tilde{d}_R
$\hat{L} \equiv \begin{pmatrix} \hat{\nu} \\ \hat{e} \end{pmatrix}$	1		2		-1	$\begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \begin{pmatrix} \tilde{\nu}_L \\ \tilde{e}_L \end{pmatrix}$
\hat{E}	1		1		-2	e_R, \tilde{e}_R
$\hat{H}_d \equiv \begin{pmatrix} \hat{H}_d^0 \\ \hat{H}_d^- \end{pmatrix}$	1		2		-1	$\begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}, \begin{pmatrix} \tilde{H}_d^0 \\ \tilde{H}_d^- \end{pmatrix}$
$\hat{H}_u \equiv \begin{pmatrix} \hat{H}_u^+ \\ \hat{H}_u^0 \end{pmatrix}$	1		2		+1	$\begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \begin{pmatrix} \tilde{H}_u^+ \\ \tilde{H}_u^0 \end{pmatrix}$

Fields	$SU(3)_C$	\times	$SU(2)_L$	\times	$U(1)_Y$
G_μ^a, \tilde{g}^a	8		1		0
W_μ^j, λ_j	1		3		0
B_μ, λ_0	1		1		0

A new symmetry? Let's break it!

- Reasons for supersymmetry breaking:
 - There are no particles with the same mass as the electron
 - Bosonic selectrons in atoms: fatal impact on chemistry

But why introduce it when it's broken?

- **Solution:** Only break mass symmetry, but keep coupling symmetry intact
- I.e. standard model and SUSY particles have different masses, but their fields transform under the same gauge symmetry with the same coupling strength

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⇒ **Soft SUSY breaking**

- Parameterize SUSY breaking as additional terms in the Lagrangian:

$$\begin{aligned}
 -\mathcal{L}_{\text{soft}} = & \tilde{Q}_{iL}^* (M_{\tilde{Q}}^2)_{ij} \tilde{Q}_{jL} + \tilde{U}_{iR}^* (M_{\tilde{U}}^2)_{ij} \tilde{U}_{jR} + \tilde{d}_{iR}^* (M_{\tilde{d}}^2)_{ij} \tilde{d}_{jR} \\
 & + A_{ij}^d H_d \epsilon \tilde{Q}_{iL} \tilde{d}_{jR}^* + A_{ij}^u H_u \epsilon \tilde{Q}_{iL} \tilde{U}_{jR}^* + \text{h.c.} \\
 & + A_{ij}^{\prime d} H_u^* \tilde{Q}_{iL} \tilde{d}_{jR}^* + A_{ij}^{\prime u} H_d^* \tilde{Q}_{iL} \tilde{U}_{jR}^* + \text{h.c.} \\
 & + M_{H_d}^2 |H_d|^2 + M_{H_u}^2 |H_u|^2 + (B\mu H_d \epsilon H_u + \text{h.c.}) \\
 & + \frac{1}{2} (M_1 \bar{\lambda}_0 P_L \lambda_0 + \text{h.c.}) + \frac{1}{2} \left(M_2 \sum_{i=1}^3 \bar{\lambda}_i P_L \lambda_i + \text{h.c.} \right) \\
 & + \frac{1}{2} (M_3 \bar{\tilde{g}}^a P_L \tilde{g}^a + \text{h.c.})
 \end{aligned}$$

- Extension of the SM Higgs sector → one additional Higgs doublet:

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \quad H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}$$

- Type II → each doublet couples to either up- or down-type quarks only
- Two vacuum expectation values (VEV) and their ratio $\tan \beta$:

$$\langle H_u \rangle = \begin{pmatrix} 0 \\ v_u \end{pmatrix}, \quad \langle H_d \rangle = \begin{pmatrix} v_d \\ 0 \end{pmatrix}, \quad \tan \beta \equiv \frac{v_u}{v_d}$$

- Yukawa terms:

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To get the fermion mass terms, replace $H_{u/d}$ by its VEV

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- Discrete symmetry that distinguishes standard model particles from SUSY particles:

$$R = (-1)^{3(B-L)+2s}$$

- Quarks, leptons, Higgs and gauge bosons: $R = +1$
- Squarks, sleptons, Higgsinos and gauginos: $R = -1$
- R-parity conservation in the MSSM has a lot of consequences:
 - R-parity violating terms are forbidden in the Lagrangian: no $(B - L)$ -violation, no proton decay
 - Standard model particles only decay into pairs of SUSY particles: distinct signatures at collider data
 - There is a *lightest supersymmetric particle (LSP)* at the end of each decay chain of a SUSY particle
 - dark matter candidate!
 - seen as missing energy at colliders

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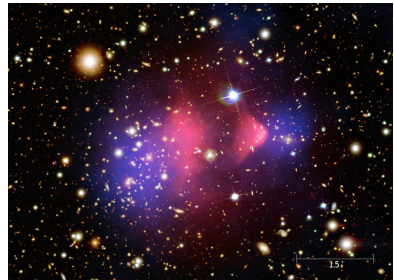
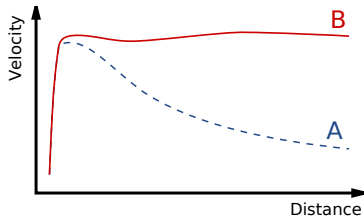
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		Value
Baryon density	Ω_b	0.044 ± 0.004
Dark matter density	Ω_χ	0.21 ± 0.02
Total matter density	Ω_m	0.26 ± 0.02
Dark energy density	Ω_Λ	0.74 ± 0.03
Photon density	Ω_γ	$(4.8 \pm 0.4) \cdot 10^{-5}$
Neutrino density	Ω_ν	$0.0009 < \Omega_\nu < 0.048$
Total energy density of the universe	Ω_{tot}	1.006 ± 0.006

Why dark?

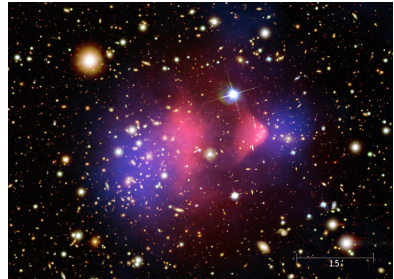
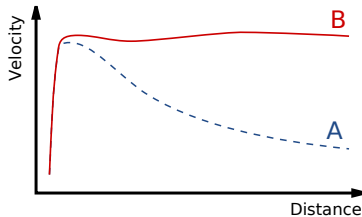
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(source for pictures: Wikipedia)

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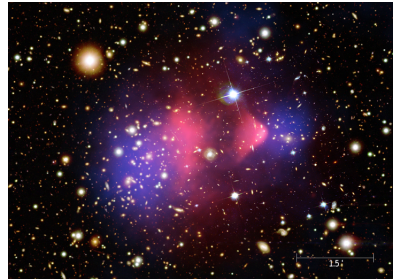
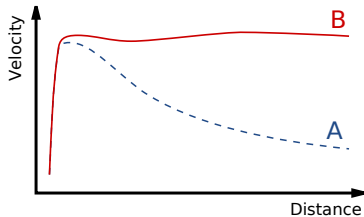
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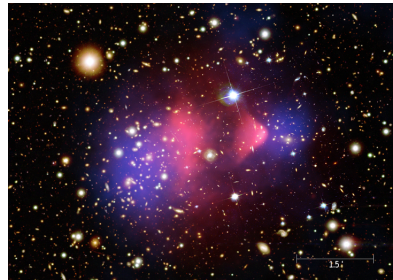
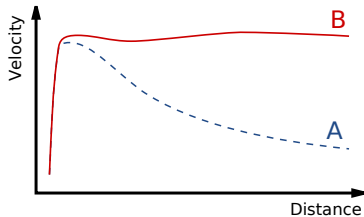
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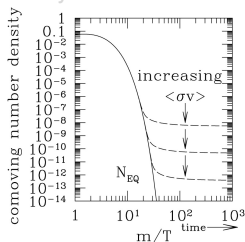


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■ Short history on dark matter (DM):

- 1) After big bang, when universe is still hot, DM particles annihilate into *lighter* SM particles and vice versa; **equilibrium**
- 2) Not enough thermal energy to produce DM particles, only process is **DM annihilation**
- 3) DM **freezes out** when the expansion of the universe is fast enough

■ Today's amount of dark matter strongly depends on annihilation mechanism



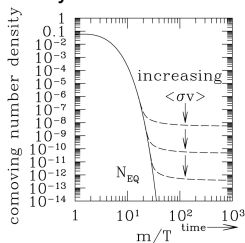
(source: <http://ned.ipac.caltech.edu/>)

■ Relic density approximation for a radiation dominated universe:

$$\Omega_\chi h^2 \sim \frac{10^{-10}}{\langle \sigma v \rangle} \text{ GeV}^{-2}$$



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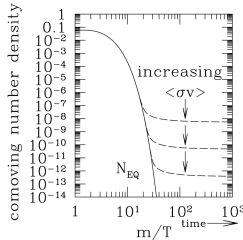
(source: <http://ned.ipac.caltech.edu/>)

- Relic density approximation for a radiation dominated universe:

$$\Omega_\chi h^2 \sim \frac{10^{-10}}{\langle \sigma v \rangle} \text{ GeV}^{-2}$$



- Short history on dark matter (DM):
 - 1) After big bang, when universe is still hot, DM particles annihilate into *lighter* SM particles and vice versa; **equilibrium**
 - 2) Not enough thermal energy to produce DM particles, only process is **DM annihilation**
 - 3) DM **freezes out** when the expansion of the universe is fast enough
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- Additional **holomorphic** and **non-holomorphic** couplings to tree level THDM couplings of type II
- With $\epsilon_{12} = 1$,

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} = \begin{pmatrix} H^+ \cos \beta \\ v_u + \frac{1}{\sqrt{2}} (H^0 \sin \alpha + h^0 \cos \alpha + iA^0 \cos \beta) \end{pmatrix},$$

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- Extract down part (since we are interested in an effective b - s - H_k^0 coupling):

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- Mass terms non-diagonal! Effective contributions render the couplings flavor-changing
- Rotate the quark fields back into physical basis with a rotation in flavor space:

$$m_{fi}^d = \left[(Y_i^d \delta_{fi} + E_{fi}^d) + E_{fi}'^d \tan \beta \right] v_d$$

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Effective couplings (3)

$$\blacksquare \mathcal{L}_Y^{\text{eff}} \supset -\bar{d}_{fL} \left[\frac{m_{d_i}}{v_d} \delta_{fi} c_k + \tilde{E}_{fi}^{'d} d_k \right] H_k^0 d_{iR} + \text{h.c.}$$

with $H_k^0 = (H^0, h^0, A^0)_k$, $\tilde{E}_{fi}^{'d} = U_{mf}^{dL*} E_{mn}^{'d} U_{ni}^{dR}$, and

$$c_k = \frac{1}{\sqrt{2}} \begin{pmatrix} \cos \alpha \\ -\sin \alpha \\ -i \sin \beta \end{pmatrix}_k, \quad d_k = \frac{1}{\sqrt{2} \cos \beta} \begin{pmatrix} \sin(\alpha - \beta) \\ \cos(\alpha - \beta) \\ i \end{pmatrix}_k.$$

- Perturbative diagonalization: U^{dL} and U^{dR} have small off-diagonal entries, can be expressed through effective couplings, e.g.

$$\tilde{E}_{23}^{'d} \approx E_{23}^{'d} - \frac{E_{33}^{'d} (E_{23}^d v_d + E_{23}^{'d} v_u)}{m_{d_3}}$$

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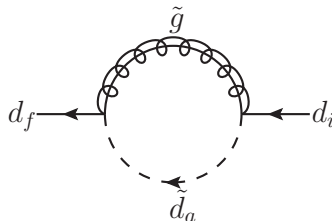
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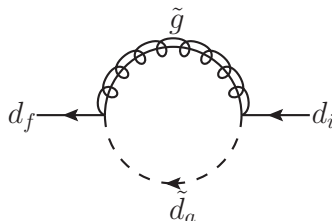


- Given as:

$$\Sigma_{fi}^d = \not{p} (\Sigma_{fi}^{dLL}(p^2)P_L + \Sigma_{fi}^{dRR}(p^2)P_R) + \Sigma_{fi}^{dRL}(p^2)P_L + \Sigma_{fi}^{dLR}(p^2)P_R$$

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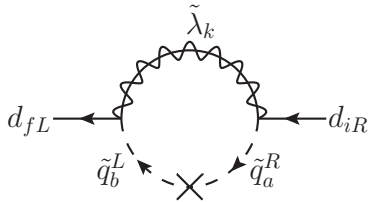
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E.g.: gluino contribution

$$\Sigma_{fi}^{dLR, \tilde{g}} = \frac{2\alpha_s}{3\pi} m_{\tilde{g}} \sum_{a=1}^6 W_{fa}^{\tilde{d}L} W_{ia}^{\tilde{d}R*} B_0(m_{\tilde{g}}^2, m_{d_a}^2)$$

- The mixing matrices W^d depend on the squark matrix elements, in the decoupling limit ($M_{\text{SUSY}} \gg v$) to only one power of the matrix element

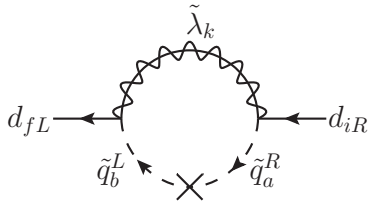


→ Mass insertion in squark line with the corresponding flavor changing matrix element

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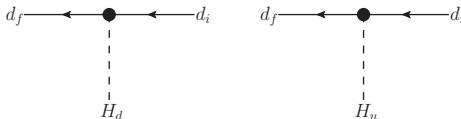
$$\mathcal{M}_{\tilde{d}}^2 = \begin{pmatrix} (\mathcal{M}_{LL}^{\tilde{d}})^2 & \Delta^{d,LR} \\ \Delta^{d,RL} & (\mathcal{M}_{RR}^{\tilde{d}})^2 \end{pmatrix} :$$

$$\Sigma_{fi}^{dLR, \tilde{g}} \stackrel{(\text{dec.})}{=} \frac{2\alpha_s}{3\pi} m_{\tilde{g}} \sum_{a,b=1}^3 \sum_{l,m=1}^3 W_{fa}^{\tilde{d}L} W_{la}^{\tilde{d}L*} \Delta_{lm}^{d,LR} W_{mb}^{\tilde{d}R} W_{ib}^{\tilde{d}R*} \\ \times C_0(m_{\tilde{g}}^2, m_{\tilde{d}_a^L}^2, m_{\tilde{d}_b^R}^2)$$

- The chirality-changing matrix element is given as

$$\Delta_{ij}^{d,LR} = v_d A_{ij}^d - v_u \mu Y_i^d \delta_{ij}$$

Effective couplings in the MSSM



- Replace E^d and E'^d with contributions from $\Sigma^{dLR, \tilde{g}}$:

$$E_{fi}^d = \frac{1}{v_d} \Sigma_{fi A}^{dLR}, \quad E_{fi}'^d = \frac{1}{v_u} \Sigma_{fi \mu}^{dLR}$$

- Write down new effective coupling:

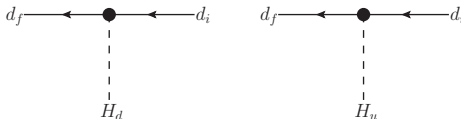
$$\Gamma_{d_i d_i}^{H_k^{0, LR}} = \frac{1}{v_d} \left[x_k^d m_{d_i} \delta_{fi} + y_k^d \tilde{\Sigma}_{fi \mu}^{dLR} \right] = \frac{1}{v_d} \left[x_k^d m_{d_i} \delta_{fi} + y_k^d \left(\Sigma_{fi \mu}^{dLR} - \frac{\Sigma_{ii \mu}^{dLR}}{m_{d_i}} \Sigma_{fi}^{dLR} \right) \right]$$

with

$$x_k^d = \frac{1}{\sqrt{2}} (-\cos \alpha, \sin \alpha, i \sin \beta)_k, \quad y_k^d = -\frac{\sin \beta}{\sqrt{2}} (\sin(\alpha - \beta), \cos(\alpha - \beta), i)_k$$



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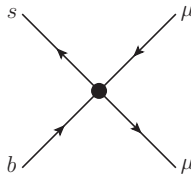
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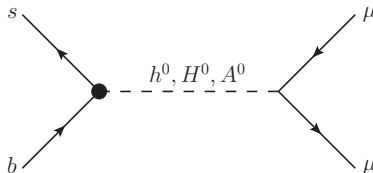
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Wilson coefficients

- Effective coupling with the Wilson coefficients as the coupling strength:



- From leading contribution



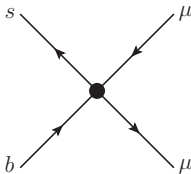
the scalar and pseudoscalar Wilson coefficients can be calculated:

$$C_S = -C_P = -\frac{2\pi m_\mu \tan^2 \beta}{\alpha m_b M_{A^0}^2 V_{ts}^* V_{tb}} \left(\Sigma_{23 \mu}^{dLR} - \frac{\Sigma_{33 \mu}^{dLR}}{m_b} \Sigma_{23}^{dLR} \right)$$

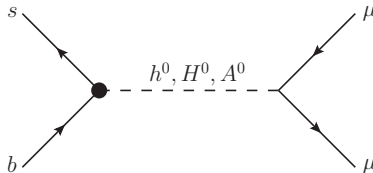


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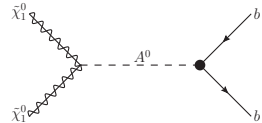
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- Relic density: $\Omega_\chi h^2 \propto 1/\langle\sigma v\rangle \propto M_{A^0}^4/\tan^2\beta$
- Parameterization of the NMFV sources in $\Delta_{ij}^{d,LR}$:

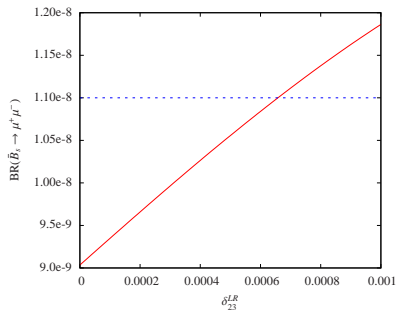
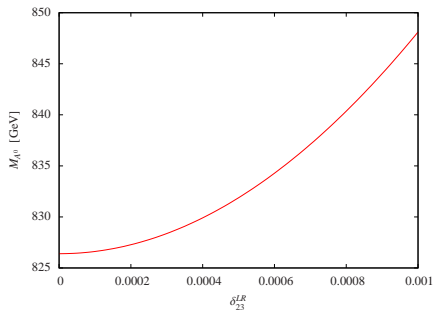
$$\delta_{ij}^{d,LR} = \frac{\Delta_{ij}^{d,LR}}{\sqrt{\left(\mathcal{M}_{LL}^{\tilde{d}}\right)_{ii}^2 \left(\mathcal{M}_{RR}^{\tilde{d}}\right)_{jj}^2}}$$

- High $\tan\beta = 50 \rightarrow$ Higgs funnel region

Input parameters

- Higgs mass for h^0 : 115.5 GeV [ATLAS; arXiv:1202.1408]
- Top pole mass: 172.9 GeV [PDG '11]
- $\text{BR}(\bar{B}_s \rightarrow \mu^+ \mu^-) < 1.1 \times 10^{-8}$ [CMS; arXiv:1201.4257]
- Relic density: $0, 0997 \leq \Omega_\chi h^2 \leq 0, 1221$ [WMAP 7-year-data]

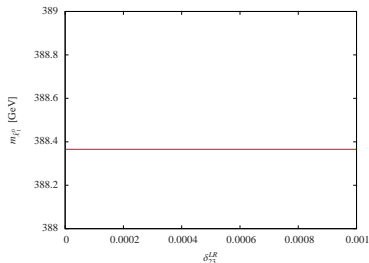
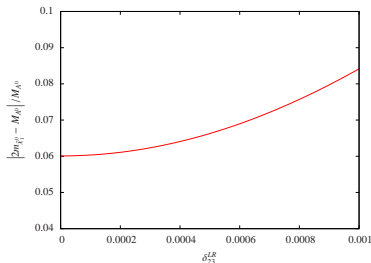
Dependence on $\delta_{23}^{d,LR}$ (1)



Input:

$m_0 = 780$ GeV, $m_{1/2} = 910$ GeV, $\tan \beta = 50$ GeV, $\text{sign}(\mu) > 0$, $A_0 = 0$ GeV

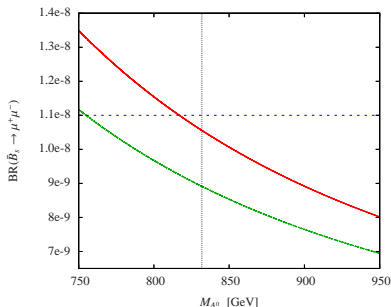
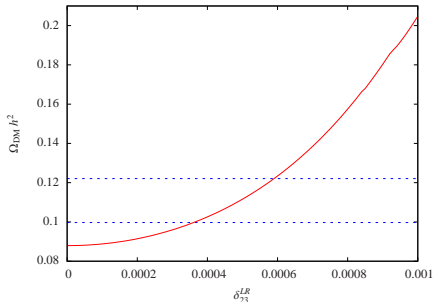
Dependence on $\delta_{23}^{d,LR}$ (2)



Input:

$m_0 = 780$ GeV, $m_{1/2} = 910$ GeV, $\tan \beta = 50$ GeV, $\text{sign}(\mu) > 0$, $A_0 = 0$ GeV

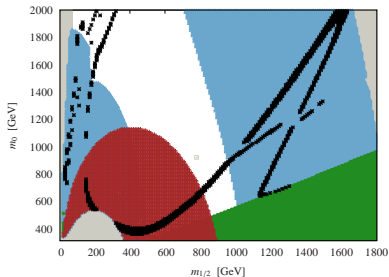
Dependence on $\delta_{23}^{d,LR}$ (3)



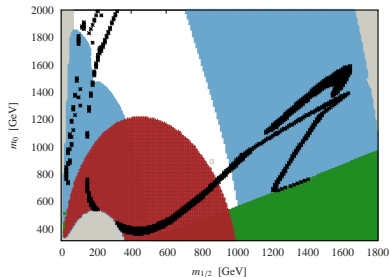
Input:

$m_0 = 780$ GeV, $m_{1/2} = 910$ GeV, $\tan \beta = 50$ GeV, $\text{sign}(\mu) > 0$, $A_0 = 0$ GeV

$$A_0 = 0 \text{ GeV}, \tan \beta = 50, \text{sign}(\mu) > 0$$

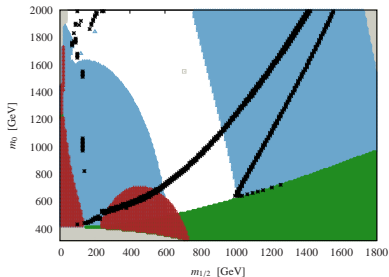


$$\delta_{23}^{d,LR} = 0$$

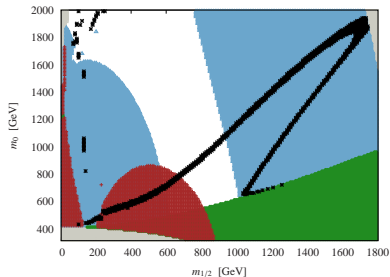


$$\delta_{23}^{d,LR} = 0.0005$$

$$A_0 = 1000 \text{ GeV}, \tan \beta = 50, \text{sign}(\mu) > 0$$

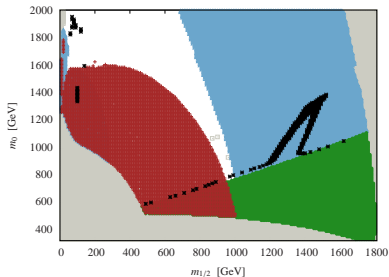


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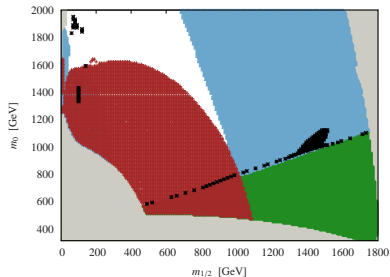


$$\delta_{23}^{d,LR} = 0.0005$$

$$A_0 = -1000 \text{ GeV}, \tan \beta = 50, \text{sign}(\mu) > 0$$



$$\delta_{23}^{d,LR} = 0$$



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- M_{A^0} has strong dependence on $\delta_{23}^{d,LR}$
 - effect on relic density and branching ratio
 - correlation between the two
- Big excluded region due to Higgs mass
- $\bar{B}_s \rightarrow \mu^+ \mu^-$ limits the little parameter space that is left for the funnel region
 - even less space available with high $\delta_{23}^{d,LR}$
- Most parameter space available in the Higgs funnel region for high positive A_0 , fewest parameter space available for high negative A_0
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- There is a need to include other rare processes such as $b \rightarrow s\gamma$ and $B_s - \bar{B}_s$ (more sensitive to $\delta_{23}^{d,LR}$?)
- Find an underlying theory to account for the size of $\delta_{23}^{d,LR}$
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Backup

Perturbative diagonalization (1)

$$U^{dL} = \begin{pmatrix} 1 & \frac{E_{12}^d v_d + E_{12}^{d*} v_u}{m_{d_2}} & \frac{E_{13}^d v_d + E_{13}^{d*} v_u}{m_{d_3}} \\ -\frac{E_{12}^{d*} v_d + E_{12}^d v_u}{m_{d_2}} & 1 & \frac{E_{23}^d v_d + E_{23}^{d*} v_u}{m_{d_3}} \\ -\frac{E_{13}^{d*} v_d + E_{13}^d v_u}{m_{d_3}} & -\frac{E_{23}^{d*} v_d + E_{23}^d v_u}{m_{d_3}} & 1 \end{pmatrix}$$

$$U^{dR} = \begin{pmatrix} 1 & \frac{E_{21}^{d*} v_d + E_{21}^d v_u}{m_{d_2}} & \frac{E_{31}^{d*} v_d + E_{31}^d v_u}{m_{d_3}} \\ -\frac{E_{21}^d v_d + E_{21}^{d*} v_u}{m_{d_2}} & 1 & \frac{E_{32}^{d*} v_d + E_{32}^d v_u}{m_{d_3}} \\ -\frac{E_{31}^d v_d + E_{31}^{d*} v_u}{m_{d_3}} & -\frac{E_{32}^d v_d + E_{32}^{d*} v_u}{m_{d_3}} & 1 \end{pmatrix}$$

Perturbative diagonalization (2)

$$\tilde{E}_{fi}'^d = U_{kf}^{dL*} E_{kl}'^d U_{li}^{dR}$$

$$\approx E_{fi}'^d - \begin{pmatrix} 0 & \frac{E_{22}'^d (E_{12}^d v_d + E_{12}'^d v_u)}{m_{d_2}} & \frac{E_{33}'^d (E_{13}^d v_d + E_{13}'^d v_u)}{m_{d_3}} \\ \frac{E_{22}'^d (E_{21}^d v_d + E_{21}'^d v_u)}{m_{d_2}} & 0 & \frac{E_{33}'^d (E_{23}^d v_d + E_{23}'^d v_u)}{m_{d_3}} \\ \frac{E_{33}'^d (E_{31}^d v_d + E_{31}'^d v_u)}{m_{d_3}} & \frac{E_{33}'^d (E_{32}^d v_d + E_{32}'^d v_u)}{m_{d_3}} & 0 \end{pmatrix}_{fi}.$$

$$\Sigma_{fi}^{dLR, \tilde{\chi}^\pm} = -\frac{Y_i^{d(0)}}{16\pi^2} \sum_{a=1}^6 \sum_{k=1}^2 \sum_{j,n=1}^3 m_{\tilde{\chi}_k^\pm} \mathcal{U}_{k2} V_{nf}^* V_{ji} \left[-g_2 \mathcal{V}_{k1} W_{na}^{\tilde{u}L} W_{ja}^{\tilde{u}L*} + Y_n^{u(0)} \mathcal{V}_{k2} W_{na}^{\tilde{u}R} W_{ja}^{\tilde{u}L*} \right] \times B_0(m_{\tilde{\chi}_k^\pm}^2, m_{\tilde{u}_a}^2)$$

$$\begin{aligned} \Sigma_{fi}^{dLR, \tilde{\chi}^0} = & -\frac{1}{16\pi^2} \sum_{a=1}^6 \sum_{k=1}^4 m_{\tilde{\chi}_k^0} \left[g_2^2 \frac{t_w}{3} \left(\frac{1}{3} Z_{k1} t_w - Z_{k2} \right) Z_{k1} W_{fa}^{\tilde{d}L} W_{ia}^{\tilde{d}R*} \right. \\ & + g_2 Y_f^{d(0)} t_w \frac{\sqrt{2}}{3} Z_{k1} Z_{k3} W_{fa}^{\tilde{d}R} W_{ia}^{\tilde{d}R*} \\ & + g_2 \frac{Y_i^{d(0)}}{\sqrt{2}} \left(\frac{1}{3} Z_{k1} t_w - Z_{k2} \right) Z_{k3} W_{fa}^{\tilde{d}L} W_{ia}^{\tilde{d}L*} \\ & \left. + Y_f^{d(0)} Y_i^{d(0)} Z_{k3}^2 W_{fa}^{\tilde{d}R} W_{ia}^{\tilde{d}L*} \right] B_0(m_{\tilde{\chi}_k^0}^2, m_{\tilde{d}_a}^2) \end{aligned}$$

Branching ratio of $\bar{B}_s \rightarrow \mu^+ \mu^-$

$$\text{BR}(\bar{B}_s \rightarrow \mu^+ \mu^-) = \frac{G_F^2 \alpha^2 M_{B_s} \tau_{B_s}}{16\pi^3} |V_{ts}^* V_{tb}|^2 \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \left\{ \left(1 - \frac{4m_\mu^2}{M_{B_s}^2}\right) |F_S|^2 + |F_P + 2m_\mu F_A|^2 \right\}$$

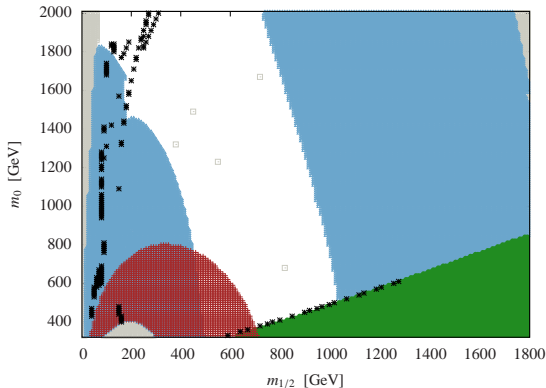
with the form factors

$$F_A = -\frac{i}{2} f_{B_s} c_A,$$

$$F_S = -\frac{i}{2} f_{B_s} M_{B_s}^2 m_b c_S,$$

$$F_P = -\frac{i}{2} f_{B_s} M_{B_s}^2 m_b c_P.$$

$$A_0 = 0 \text{ GeV}, \tan \beta = 45, \text{sign}(\mu) > 0$$



$$\delta_{23}^{d,LR} = 0.0005$$