

Static analysis

Finding bugs to building proofs

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**Programming Languages and Verification
Research Group**

Department of Computing

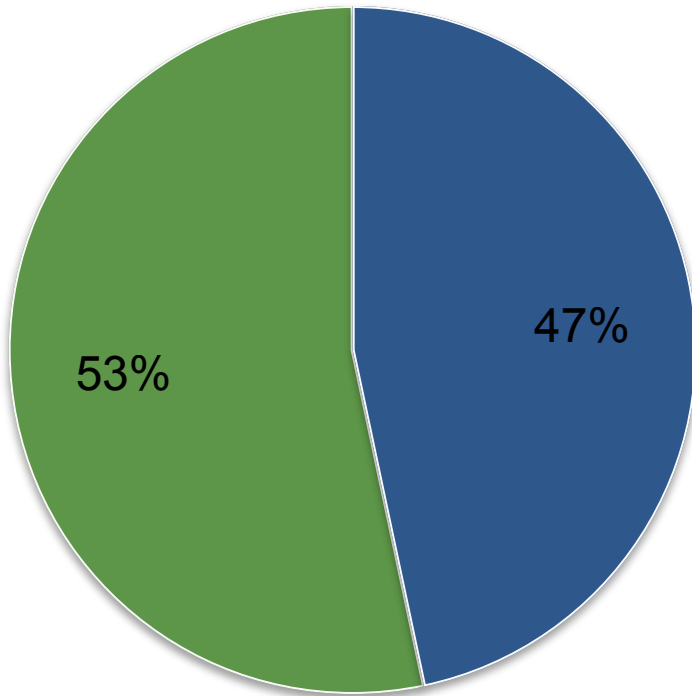


MACQUARIE
University
SYDNEY · AUSTRALIA

Commercial Static Analysers

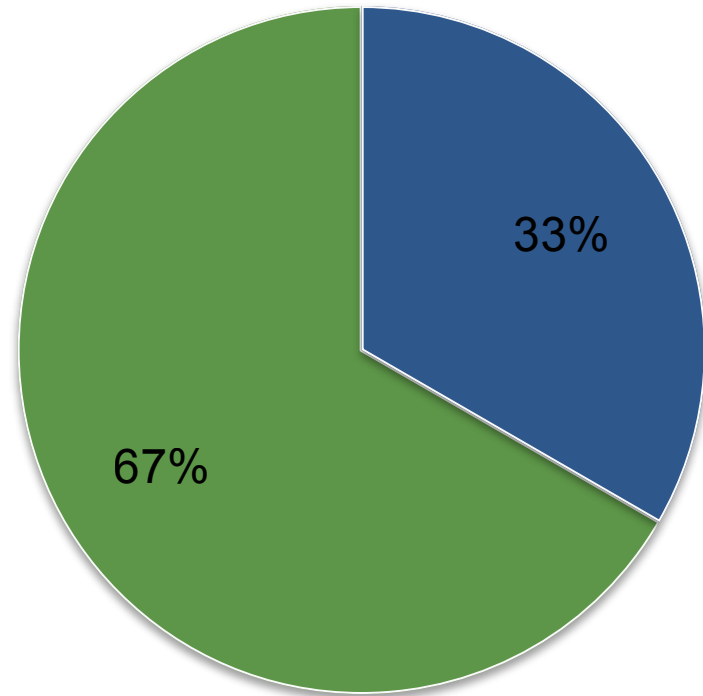
Asterisk: 30 selected

● False Positive ● True Positive



Wireshark: 30 selected

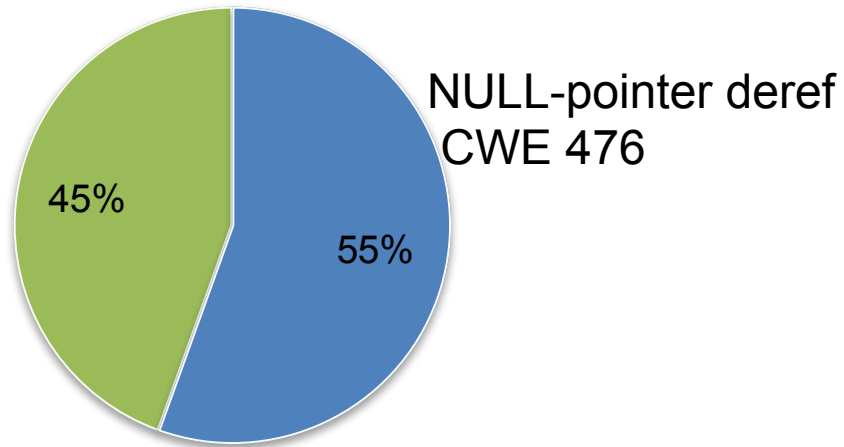
● False Positive ● True Positive



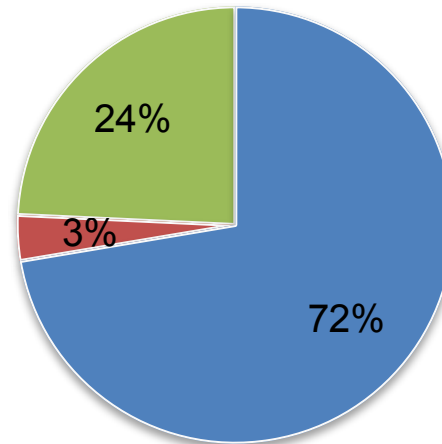
NIST SATE V Workshop, 2014

Results Juliet Test Suite (NIST)

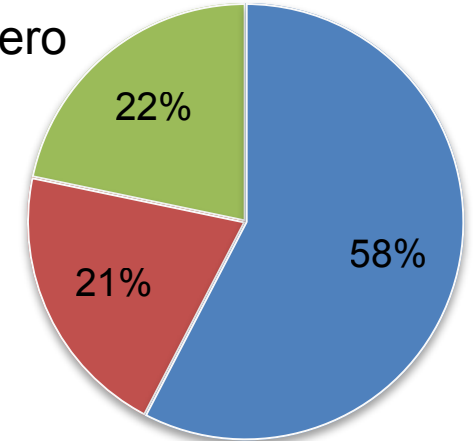
● FalseNeg ● FalsePos ● TruePos



Array-out-of-bounds
CWE 124, 126



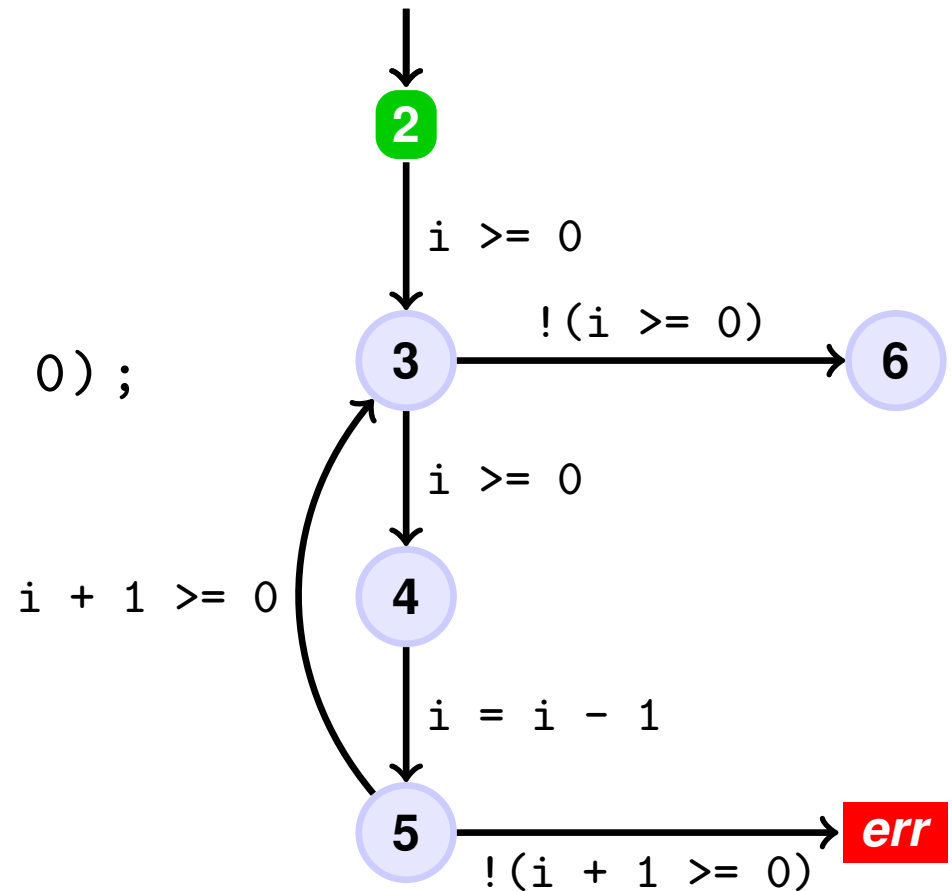
Divide-by-zero
CWE 369



NIST SATE V Workshop, 2014

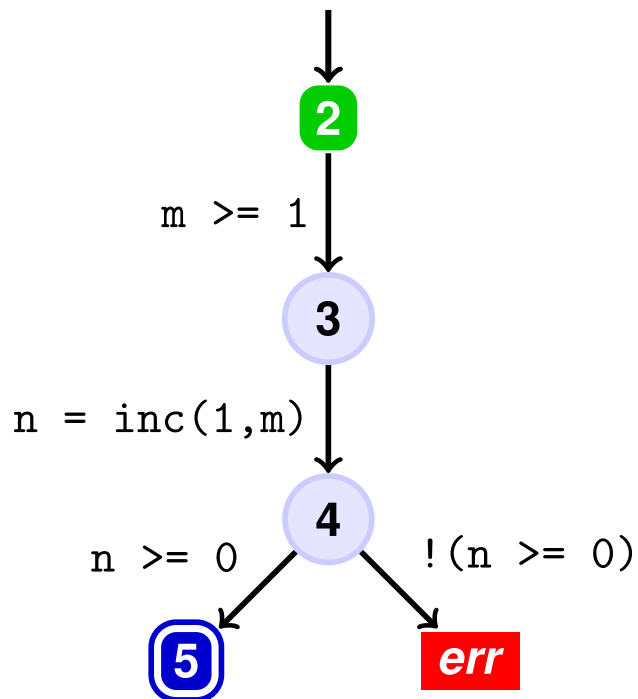
Intra-procedural

```
1  var i:int;  
2  assume i >= 0;  
3  while (i >= 0) do  
4    i = i - 1;  
5    assert (i + 1 >= 0);  
6  done;
```

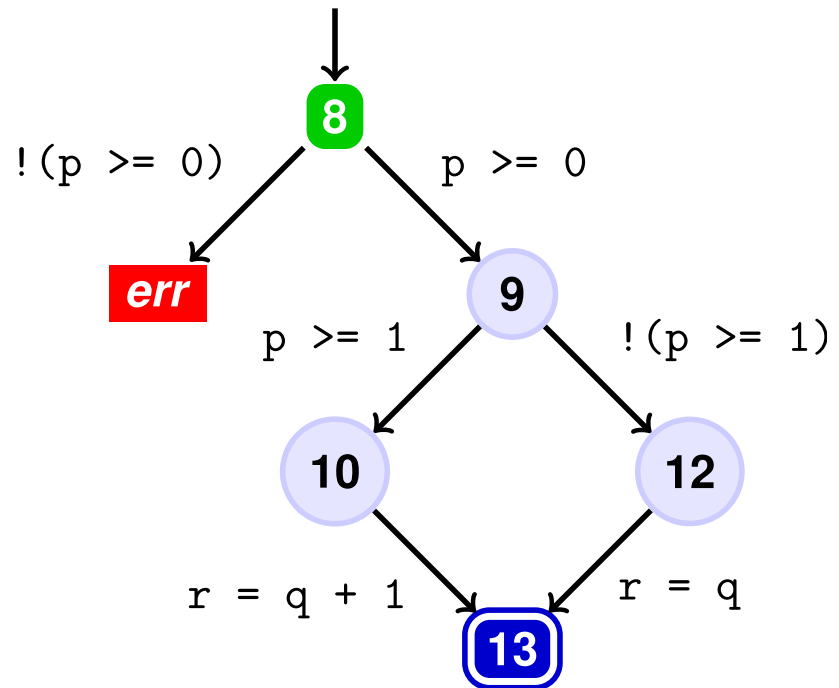


Inter-procedural

```
1  proc main() : (n) {  
2    assume(m >= 1);  
3    n = inc(1, m);  
4    assert(n >= 0);  
5  }
```



```
7  proc inc(p, q) : (r) {  
8    assert(p >= 0);  
9    if (p >= 1)  
10     r = q + 1;  
11   else  
12     r = q;  
13   endif;  
14 }
```

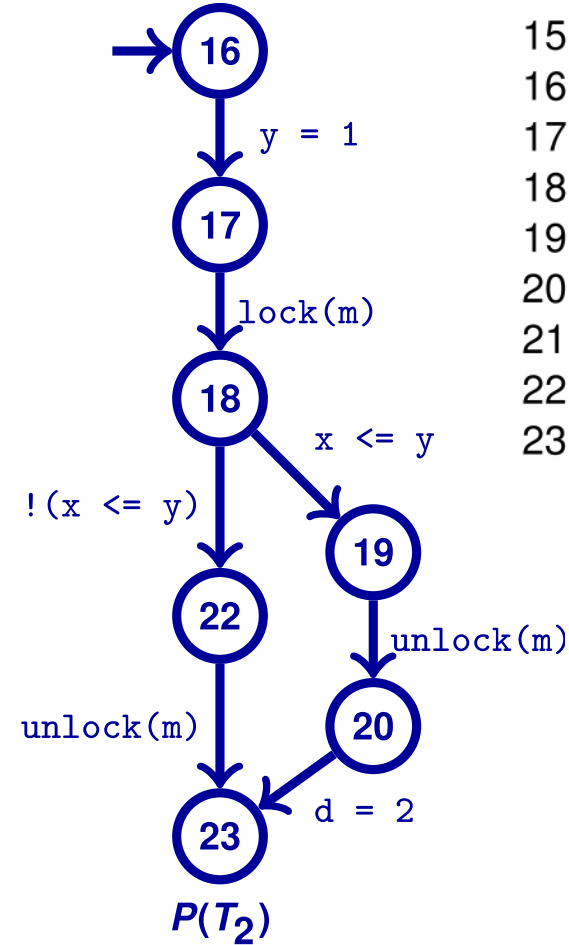
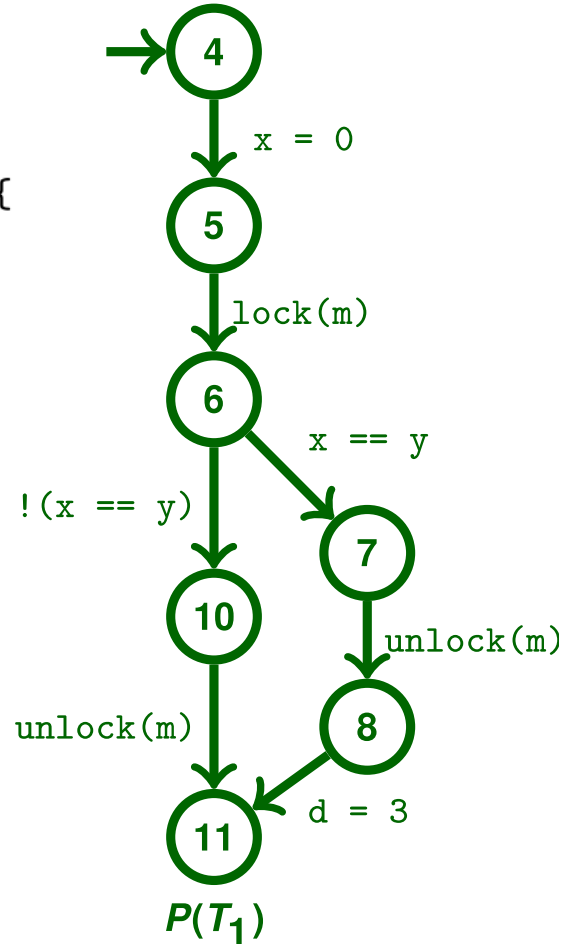


Multiple threads

```

2 // thread T1
3 thread T1
4 x = 0;
5 lock(m);
6 if (x == y) {
7     unlock(m);
8     d = 3;
9 } else {
10    unlock(m);
11 }
12 /* end */

```

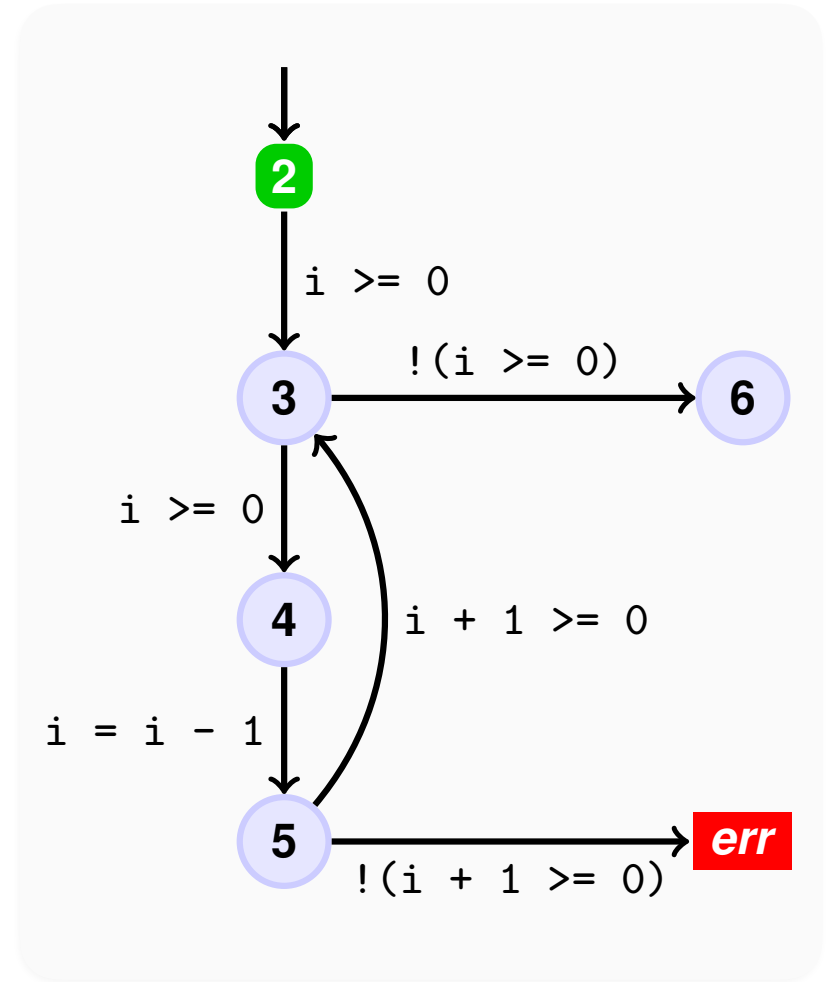
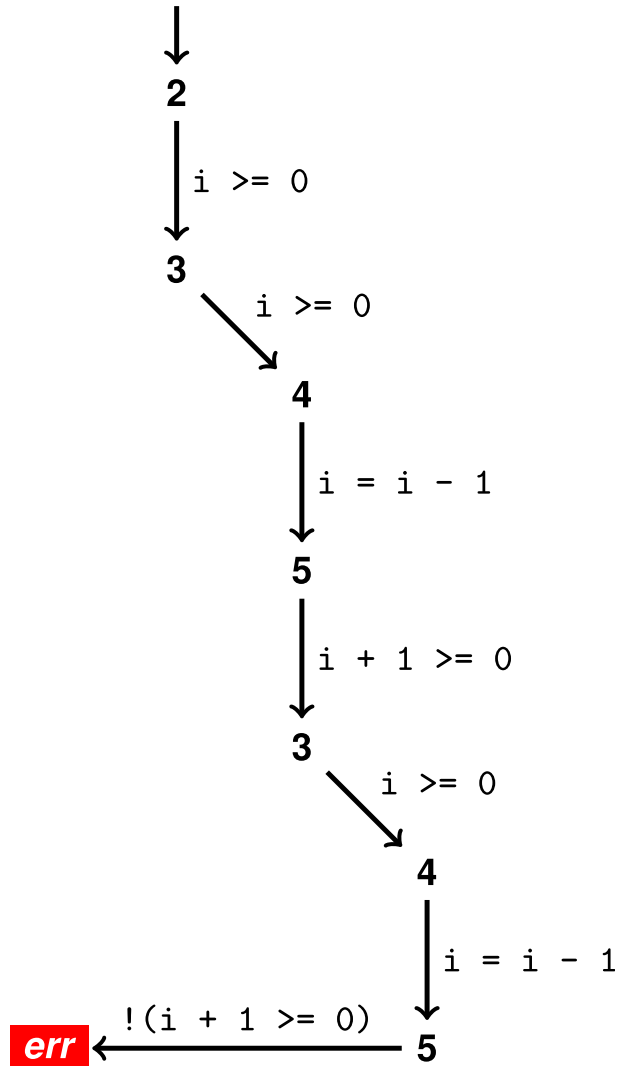
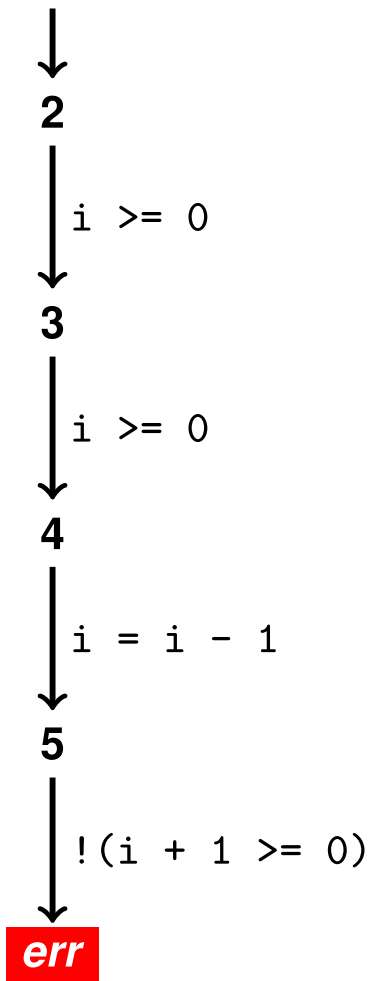


```

14 // Thread T2
15 thread T2
16 y = 1;
17 lock(m);
18 if (x <= y) {
19     unlock(m);
20     d = 2;
21 } else {
22     unlock(m);
23 }

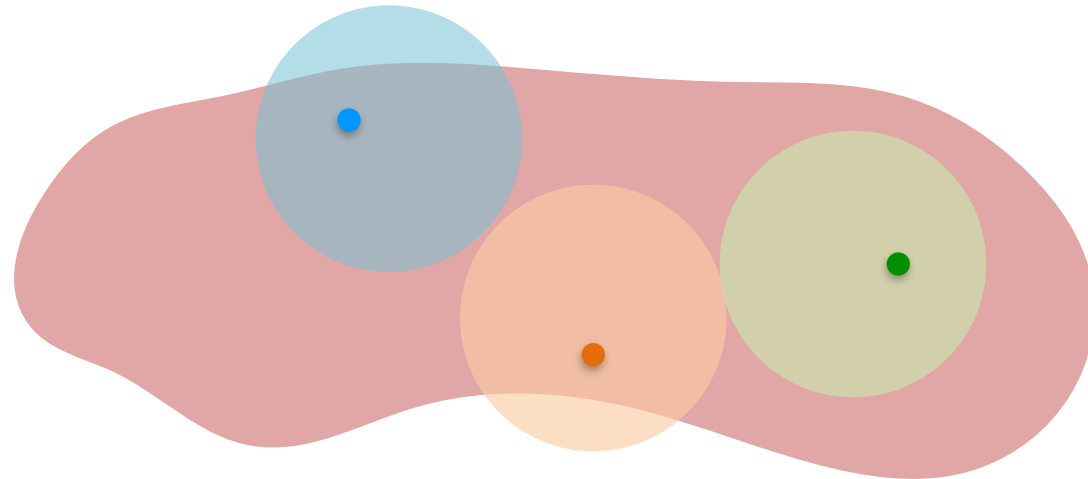
```

Trace Abstraction Refinement

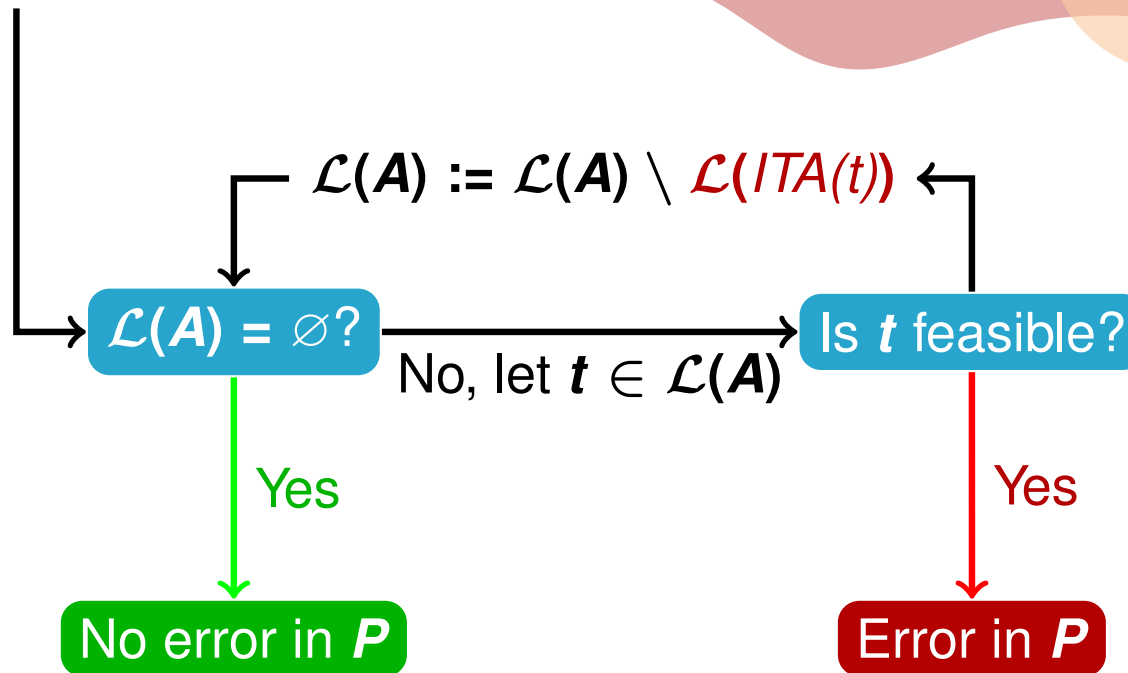


Trace Abstraction Refinement (cont'd)

Heizmann, M., Hoenicke, J., Podelski, A.
Refinement of trace abstraction.
Static Analysis Symposium, 2009.



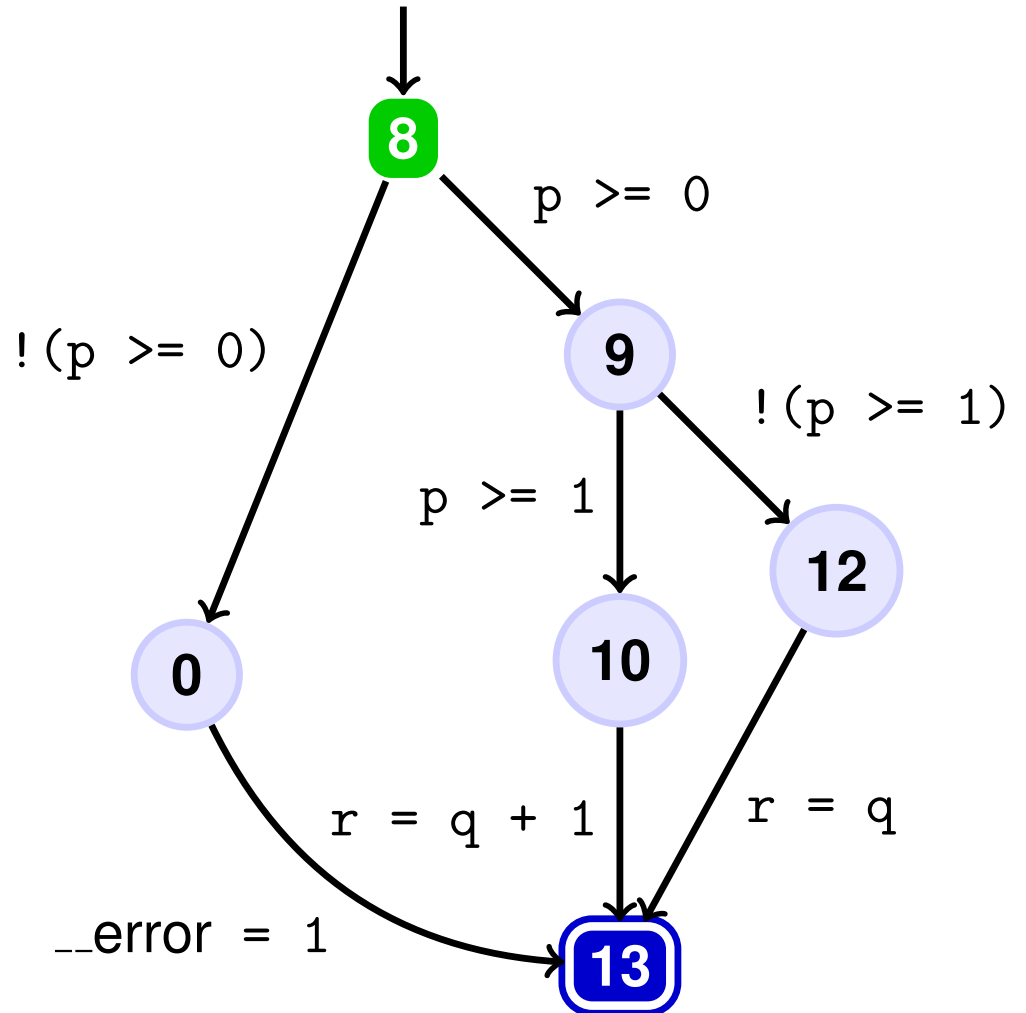
$A := CFG(P)$



Partial Correctness

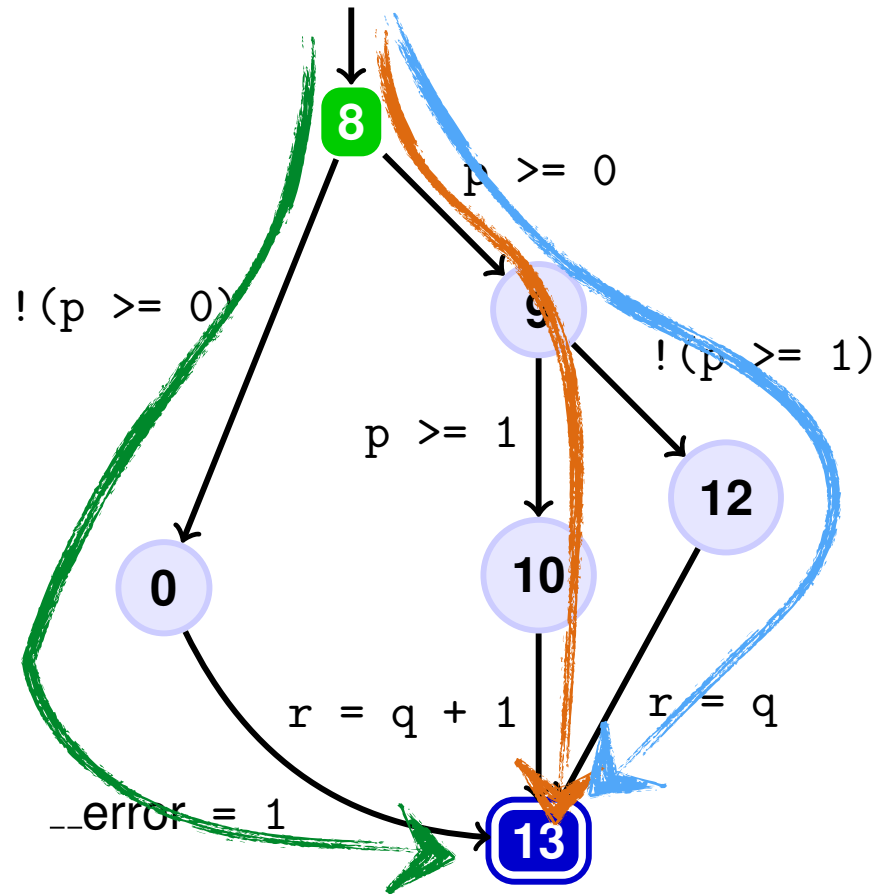
```
7  proc inc(p,q) : (r) {  
8    assert(p >= 0);  
9    if (p >= 1)  
10     r = q + 1;  
11   else  
12     r = q;  
13   endif;  
14 }
```

$\{\neg \text{__error}\} \text{ inc } \{\neg \text{__error}\}$



Building Hoare Triples

$\{p = 1 \wedge \neg \text{_error}\} \mathbf{A}_{\text{inc}} \{\neg \text{_error}\}$



$\{p \geq 0\} \rightarrow \{\neg \text{_error}\}$

$\{\neg \text{_error}\} \rightarrow \{\neg \text{_error}\}$

$\{\neg \text{_error}\} \rightarrow \{\neg \text{_error}\}$

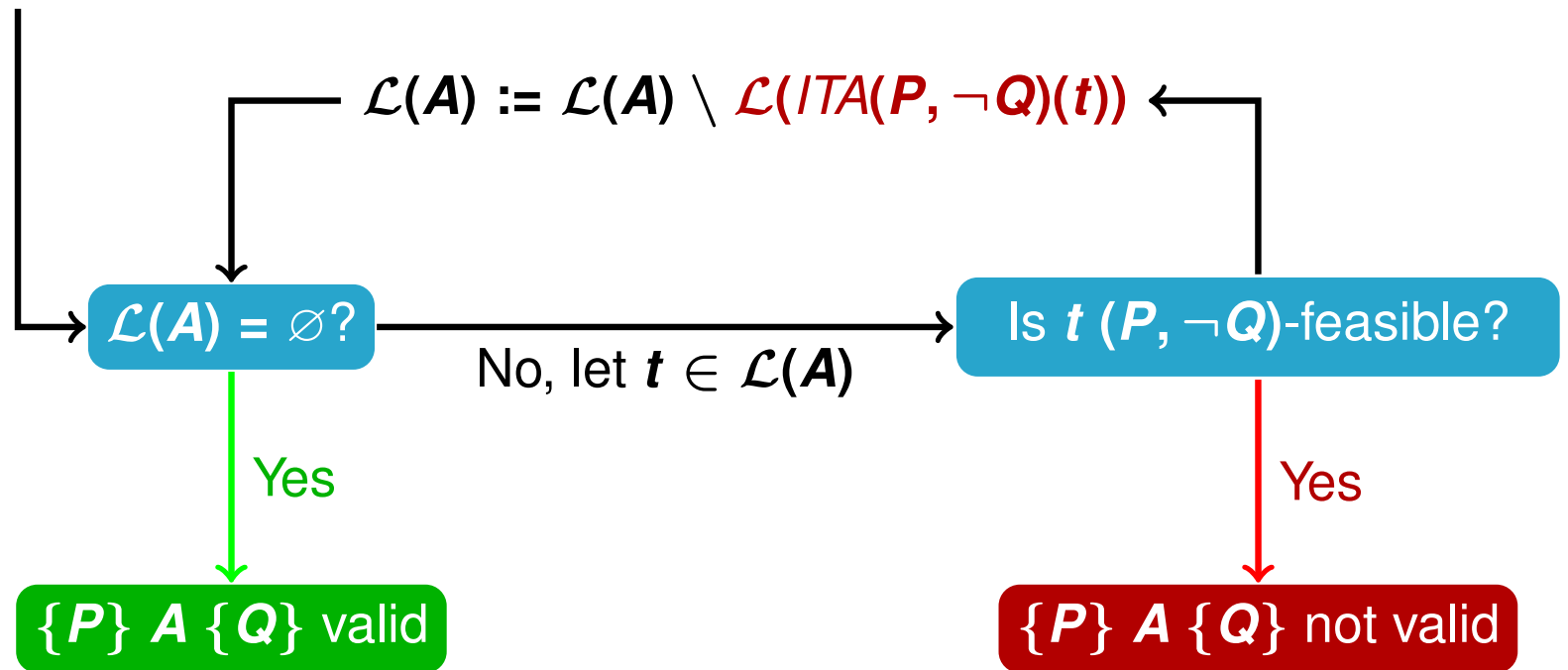
$\{p \geq 0 \wedge \neg \text{_error}\} \mathbf{A}_{\text{inc}} \{\neg \text{_error}\}$

$\{p = 1 \wedge \neg \text{_error}\} \mathbf{A}_{\text{inc}} \{\neg \text{_error}\}$

Algorithm 1

Check triple $\{P\} A \{Q\}$

$A := CFG(P)$



Found $\{P'\} A \{Q'\}$ and $P \Rightarrow P', Q' \Rightarrow Q$

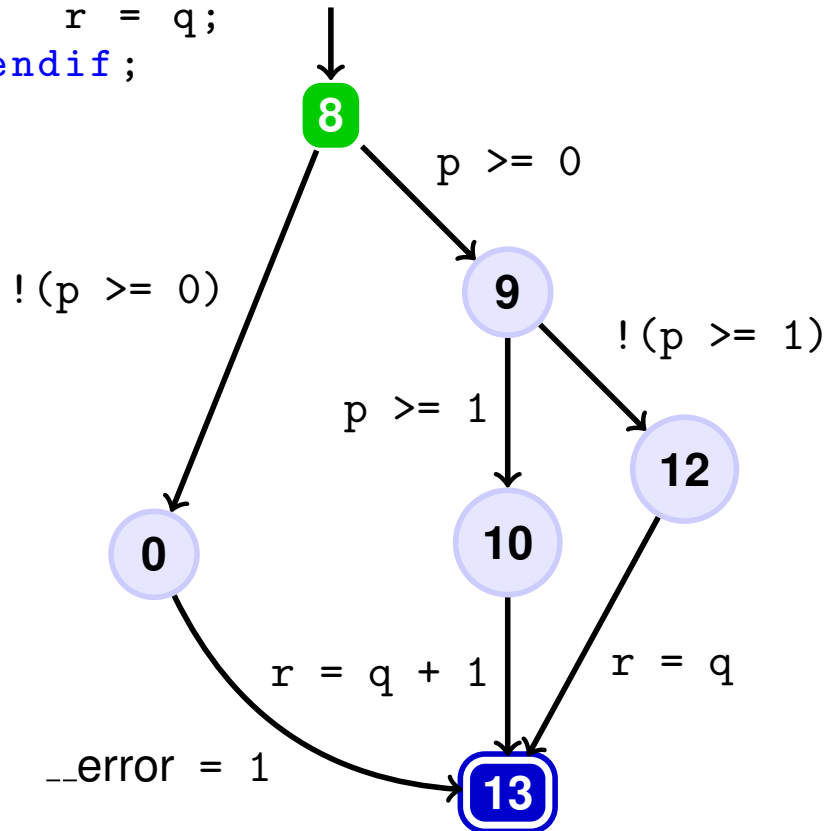
$\text{post}(t, P) \cap \neg Q \not\subseteq \text{False}$

Extended CFGs

```

7  proc inc(p,q) : (r) {
8    assert(p >= 0);
9    if (p >= 1)
10     r = q + 1;
11   else
12     r = q;
13   endif;
14 }

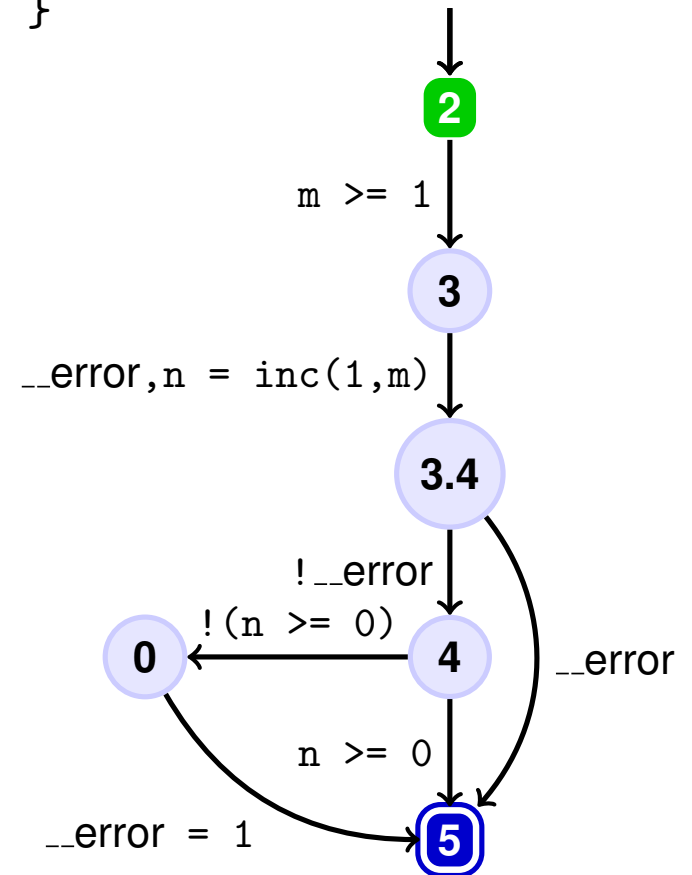
```



```

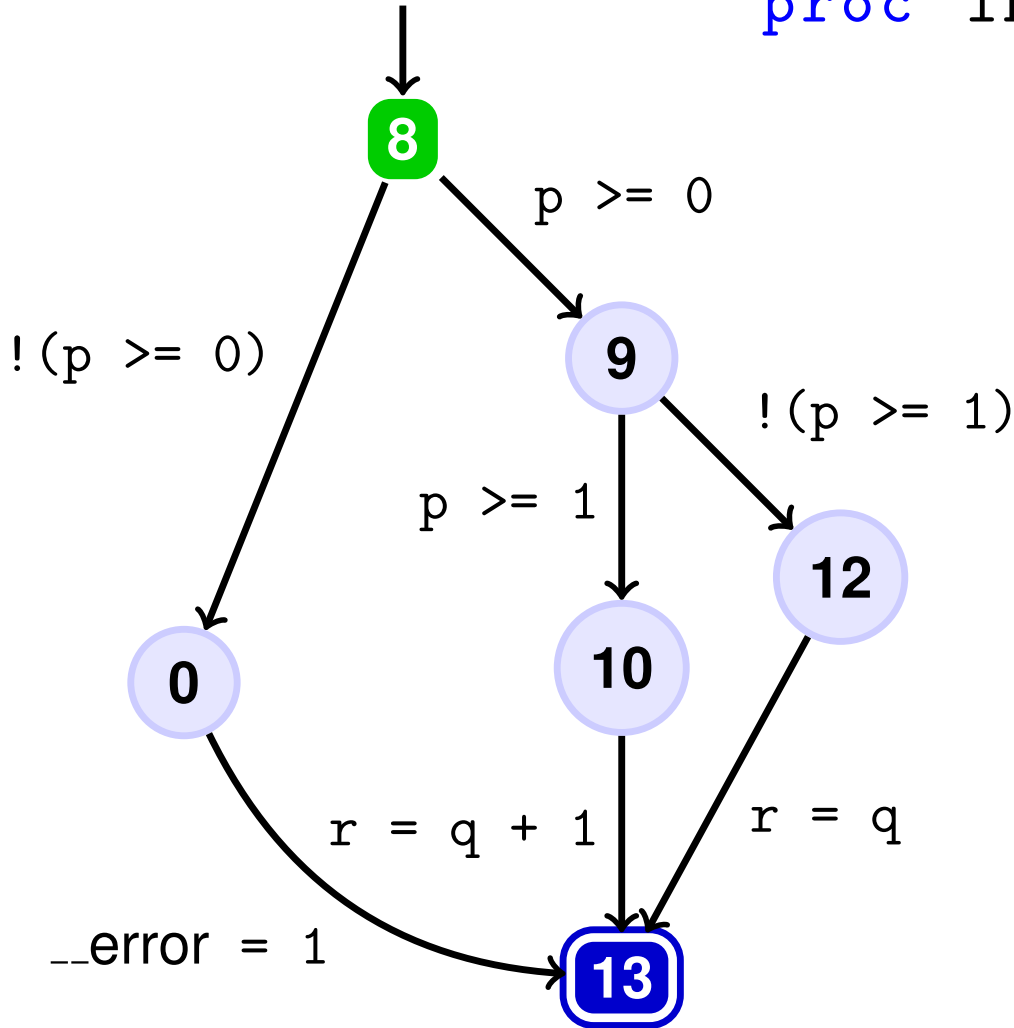
1  proc main() : (n) {
2    assume(m >= 1);
3    n = inc(1, m);
4    assert(n >= 0);
5  }

```



Function Summaries

```
proc inc(p, q) : r
```



$(p \geq 1, r \geq q + 1)$

$(p \geq 1, r \leq q + 1)$

$(p \geq 0, r > q)$

$(p \geq 1 \wedge \neg \text{error}, \neg \text{error})$

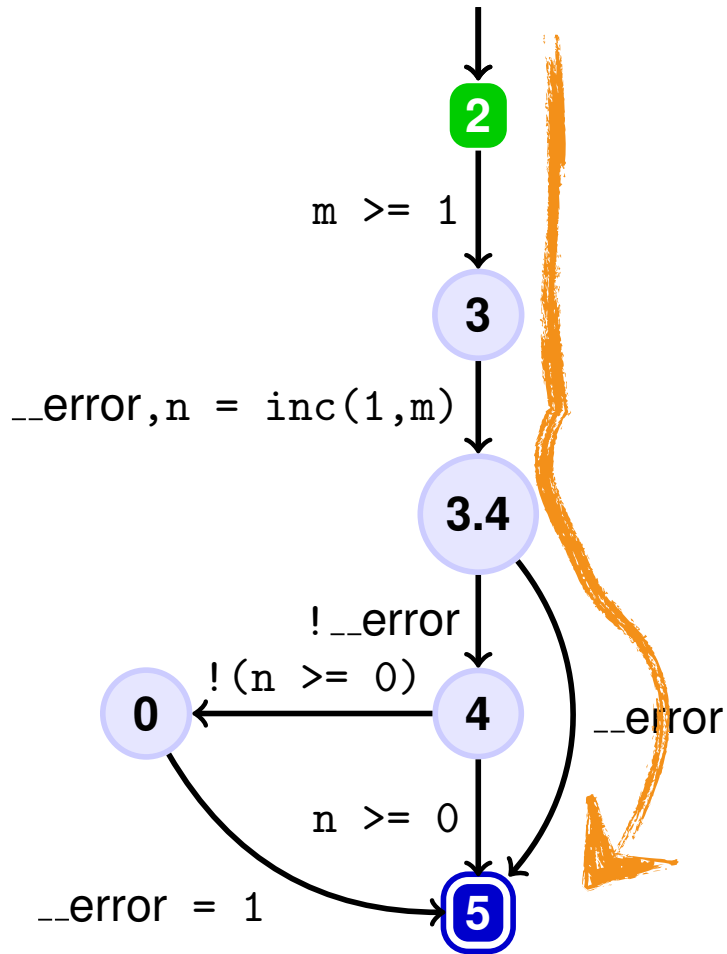
(True, True)

Inter-procedural Trace Refinement (1)

$\{\neg \text{_error}\} \mathbf{A}_{\text{main}} \{\neg \text{_error}\}$

$(\text{True}, \text{True})$

\mathbf{A}_{inc}

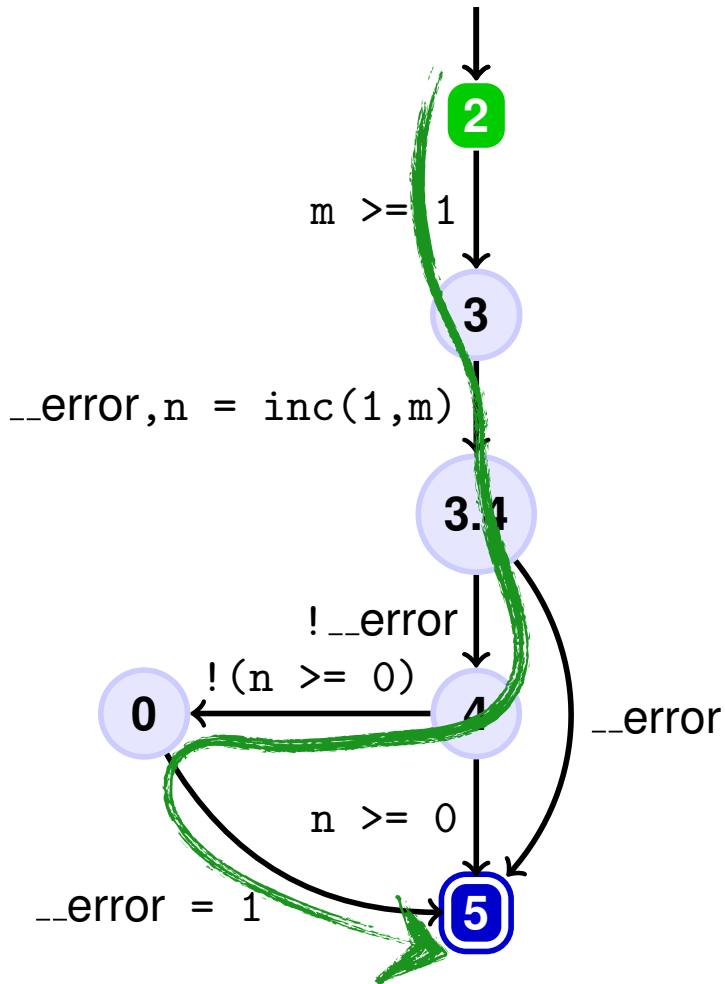


$\{\neg \text{_error} \wedge \mathbf{p} = \mathbf{q} = 1\} \mathbf{A}_{\text{inc}} \{\neg \text{_error}\}$

$\{\neg \text{_error} \wedge \mathbf{p} \geq 0\} \mathbf{A}_{\text{inc}} \{\neg \text{_error}\}$

Inter-procedural Trace Refinement (2)

$\{\neg \text{_error}\} \mathbf{A}_{\text{main}} \{\neg \text{_error}\}$



\mathbf{A}_{inc}

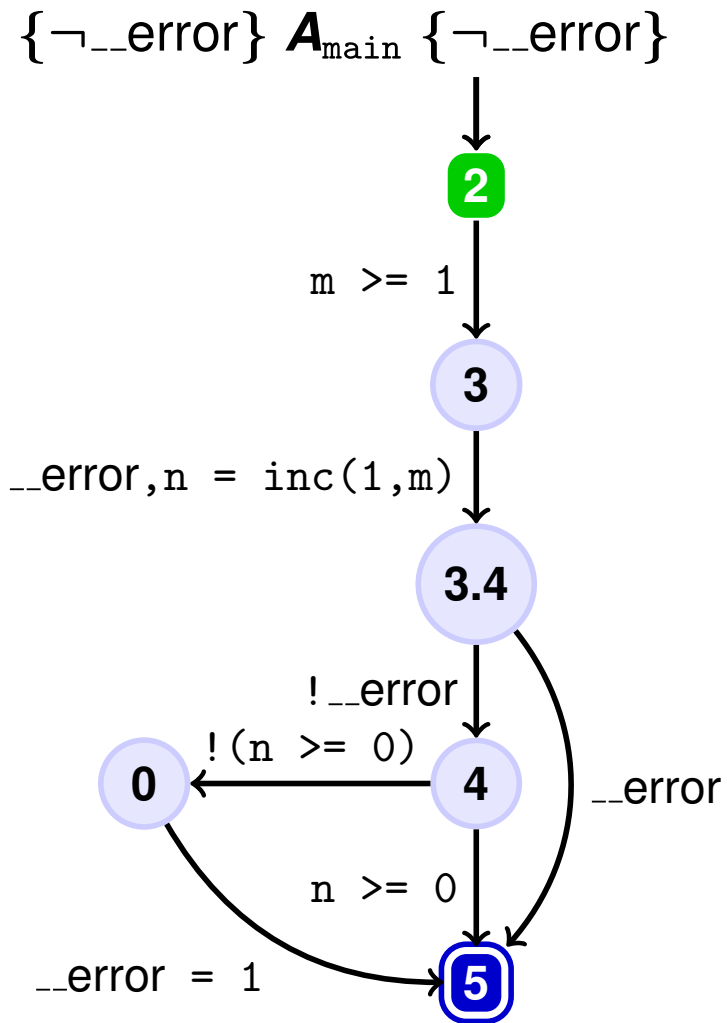
$(\text{True}, \text{True})$

$(\neg \text{_error} \wedge p \geq 0, \neg \text{_error})$

$\{p = q = 1\} \mathbf{A}_{\text{inc}} \{\text{not}(n = -1)\}$

$\{p \geq 1 \wedge q \geq 1\} \mathbf{A}_{\text{inc}} \{r \geq q + 1\}$

Inter-procedural Trace Refinement (3)



\mathbf{A}_{inc}

$(\text{True}, \text{True})$

$(\neg \text{_error} \wedge p \geq 0, \neg \text{_error})$

$(p \geq 1 \wedge q \geq 1, r \geq q + 1)$

$\{\neg \text{_error}\} \mathbf{A}_{\text{main}} \{\neg \text{_error} \wedge n \geq m + 1\}$

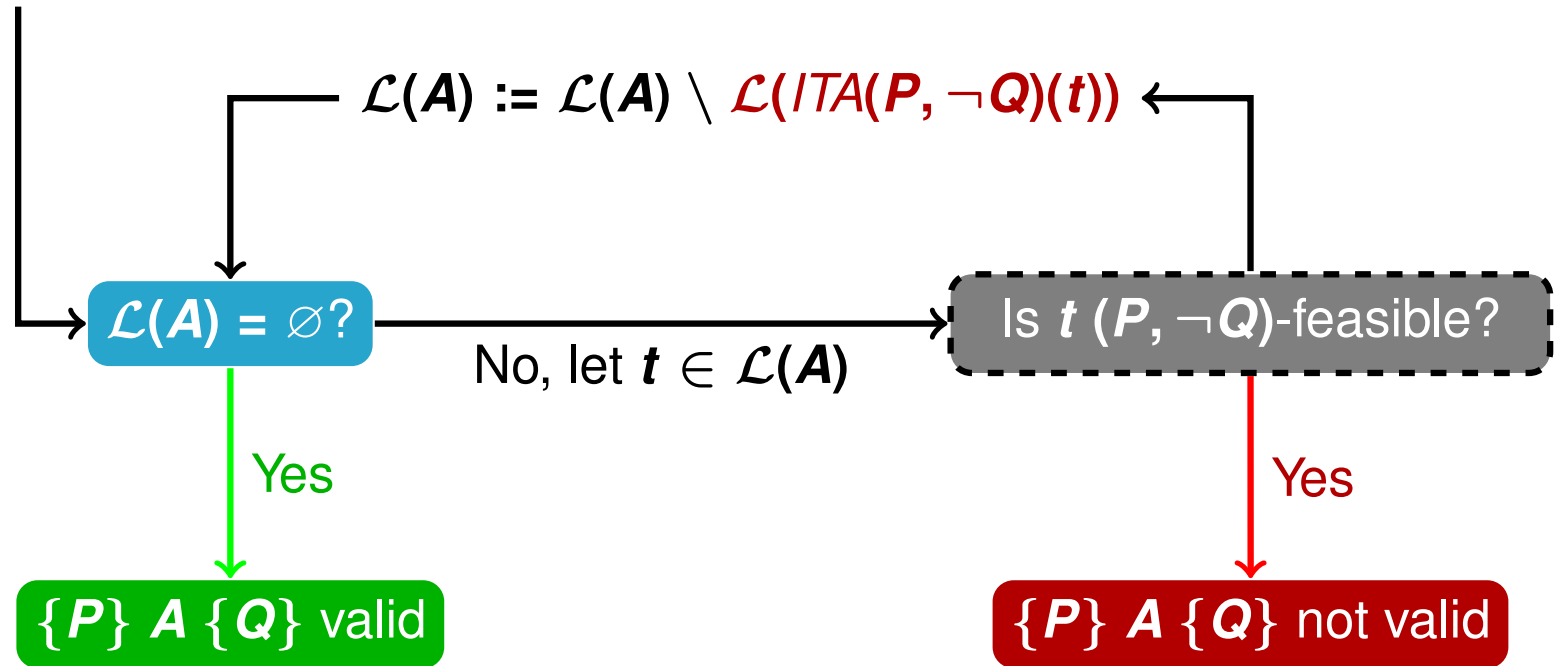
Cassez F., Müller C. and Burnett K.
 Summary-Based Inter-Procedural Analysis via
 Modular Trace Refinement, FSTTCS 2014

Cassez F. and Müller C.
 Analysis of program code
 US Patent Application (2014). 14/540,929

Algorithm 2

Check triple $\{P\} A \{Q\}$

$A := \text{CFG}(P)$



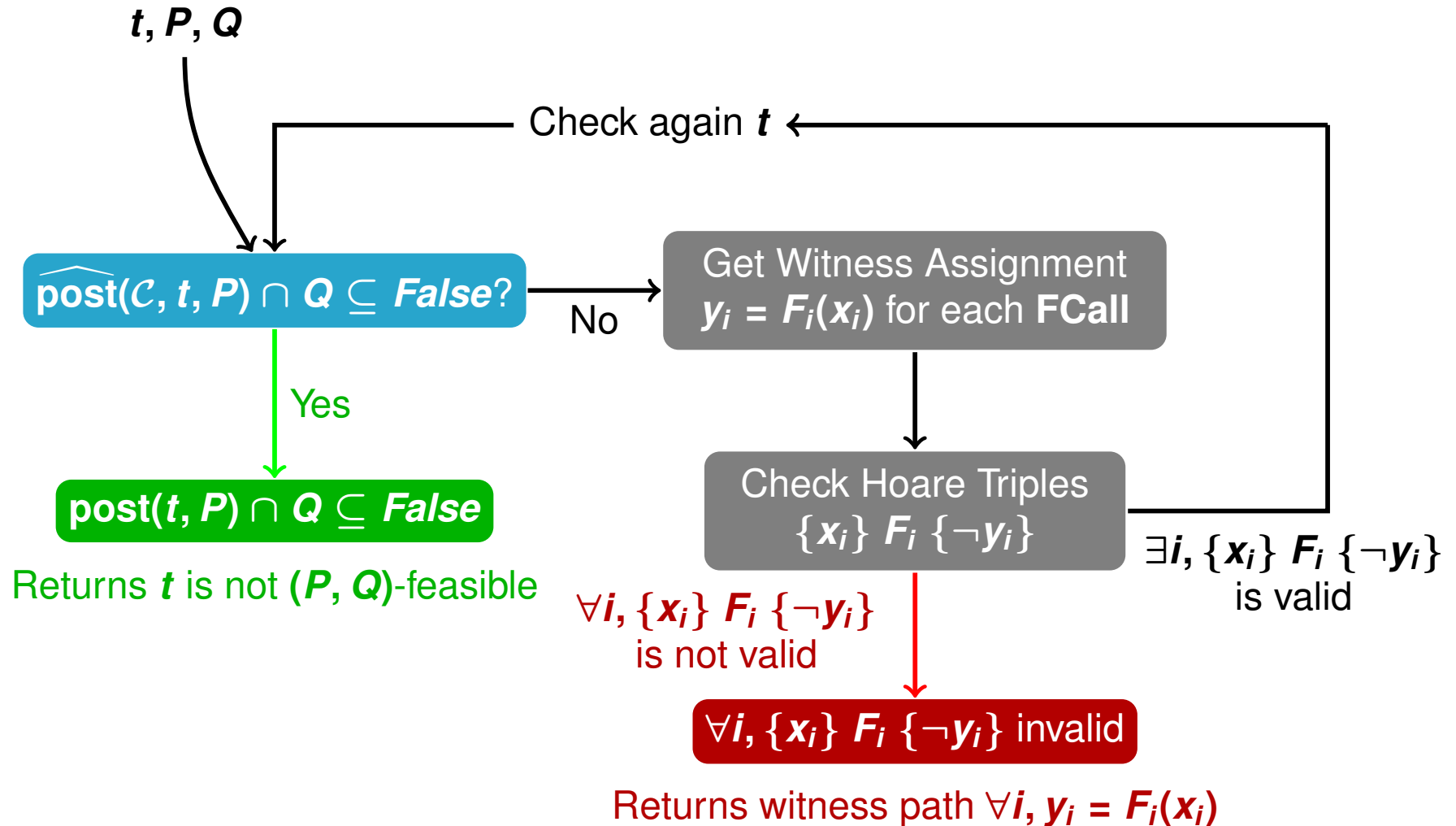
Found $\{P'\} A \{Q'\}$ and $P \Rightarrow P', Q' \Rightarrow Q$

Add (P', Q') to summary $\mathcal{C}(A)$

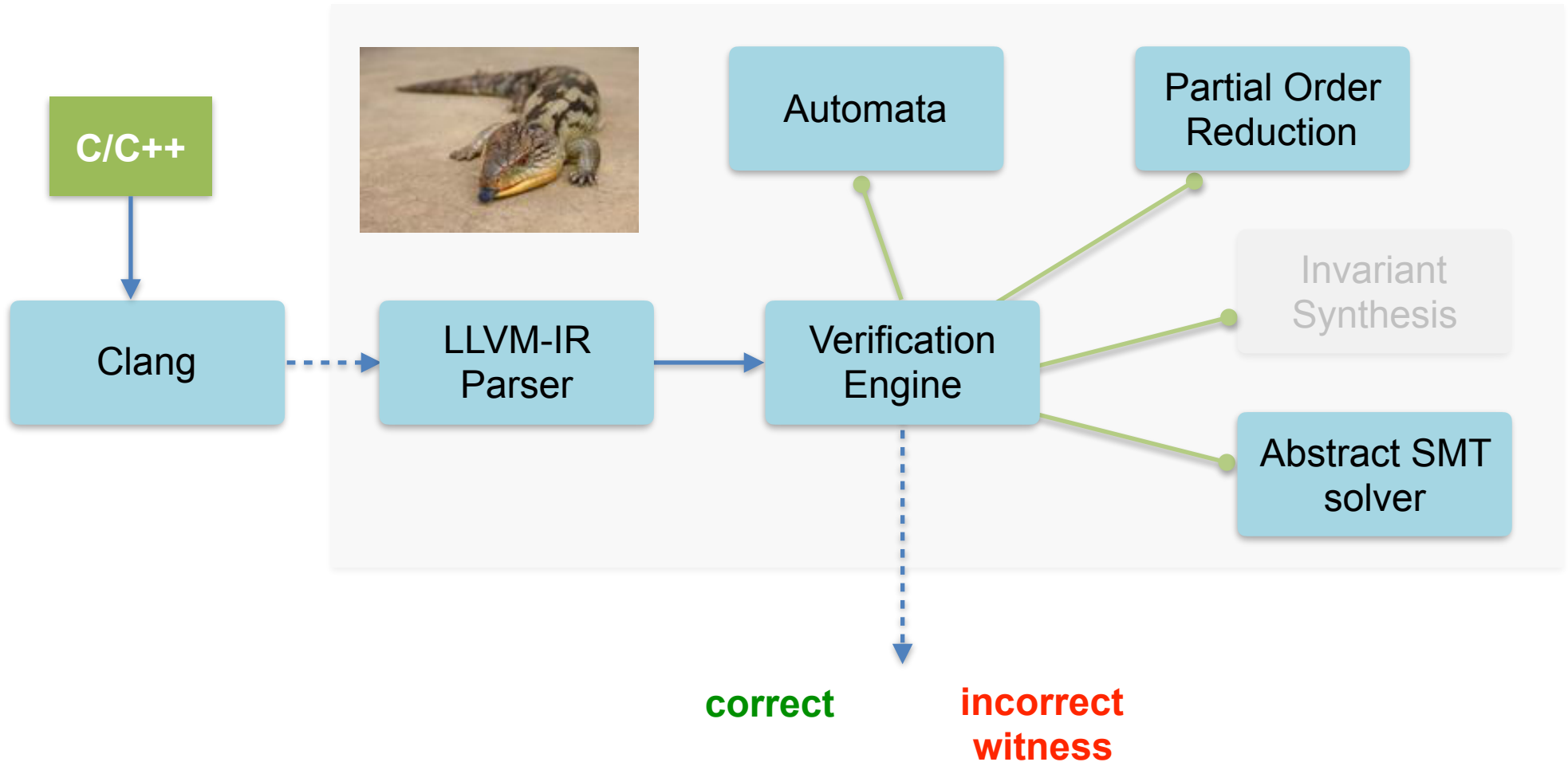
$\text{post}(t, P) \cap \neg Q \not\subseteq \text{False}$

Inter-Procedural Algorithm

Is t (P, Q) – feasible ?



Skink

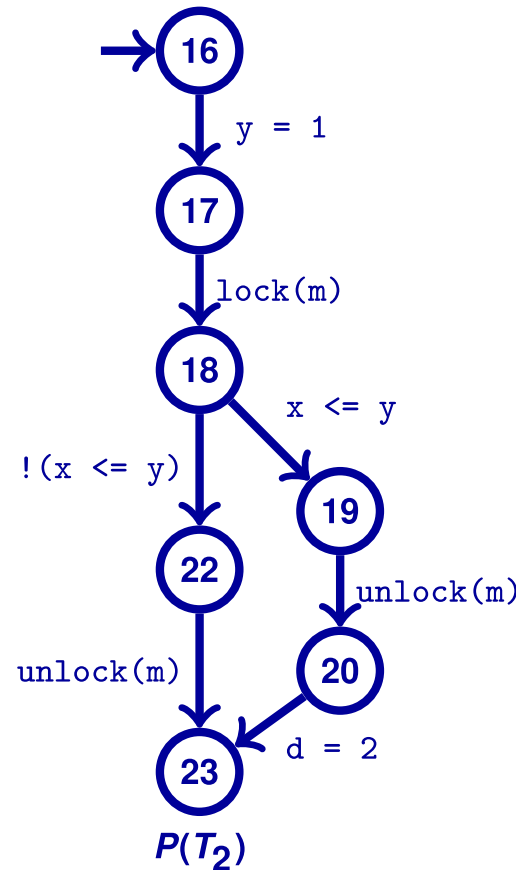
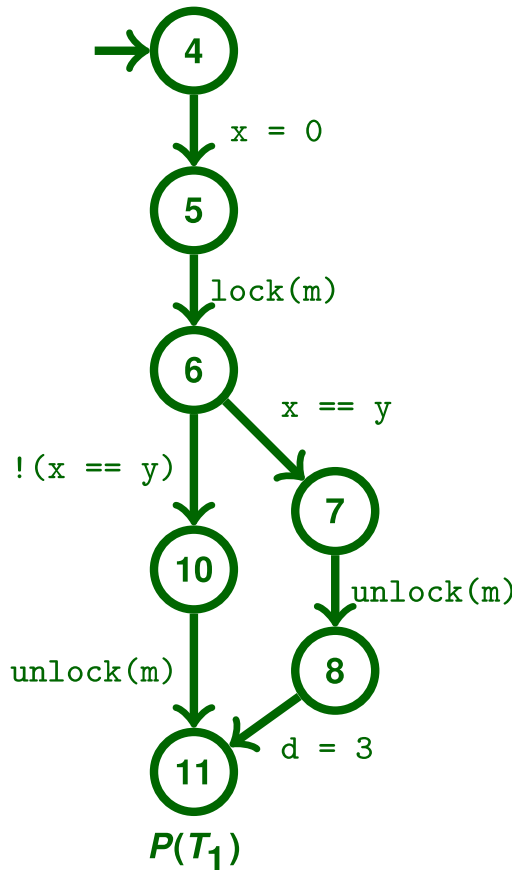


Concurrent Programs

```

2 // thread T1
3 thread T1
4 x = 0;
5 lock(m);
6 if (x == y) {
7   unlock(m);
8   d = 3;
9 } else {
10  unlock(m);
11 }
12 /* end */

```



```

14 // Thread T2
15 thread T2
16 y = 1;
17 lock(m);
18 if (x <= y) {
19   unlock(m);
20   d = 2;
21 } else {
22   unlock(m);
23 }

```

$\mathcal{L}(P(T_1) \times P(T_2))$

Is there a **feasible** error trace?

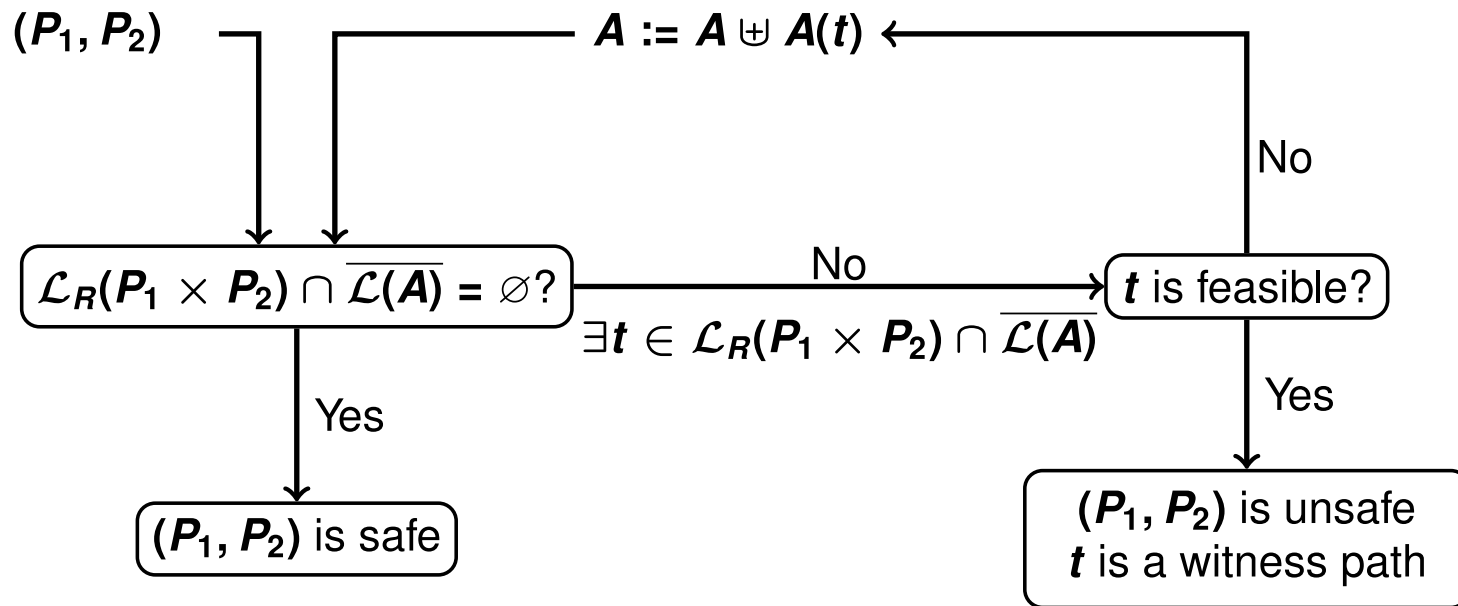
Trace Refinement for Concurrent Programs

\exists an error trace $t \in \mathcal{L}(P_1 \times P_2)$



\exists an error trace $t' \in \mathcal{L}_R(P_1 \times P_2)$

feasible



Cassez, F. and Ziegler F.
Verification of Concurrent Programs Using Trace
Abstraction Refinement
LPAR 2015