

### Automata-Based Analysis of Recursive Programs with Threads

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# Introduction

Threads & Recursion

Locks & monitors & joins

**Optimal Analysis:** 

• Complete analysis of well-specified abstract model

Regular model checking

# Reachability Analysis of Programs with Procedures and Thread Creation

### Theorem [Ramalingam]

Reachability is undecidable in programs with two threads, synchronous communication, and procedures.

### Proof:

Reduction of intersection problem  $(L_1 \cap L_2 \neq \emptyset)$  of contextfree languages  $L_1, L_2$ .

 $\Rightarrow$  abstract from synchronous communication (for now).

# A Model of Recursive Programs with Thread-creation: DPNs: Dynamic Pushdown-Networks

- A dynamic pushdown-network (DPN) over finite set of actions Act consists of:
  - P, a finite set of control symbols
  - Γ, a finite set of stack symbols
  - $\Delta$ , a finite set of rules of the following form

 $p\gamma \xrightarrow{a} p_1 w_1 \qquad [ \text{ with } |w_1| \le 2 ]$   $p\gamma \xrightarrow{a} p_1 w_1 \triangleright p_2 w_2 \qquad [ \text{ with } |w_1| = 1 \text{ and } |w_2| = 1 ]$ 

(with  $p, p_1, p_2 \in \mathsf{P}, \gamma \in \Gamma, w_1, w_2 \in \Gamma^*$ ,  $a \in \mathsf{Act}$ ).

• DPNs can model recursive programs with thread-creation primitives using finite abstractions of (thread-local) global variables and local variables of procedures.

# Execution-Semantics of DPNs on Word-Shaped Configurations

A configuration of a DPN is a word in  $(P\Gamma^*)^+$ :

 $p_1 w_1 p_2 w_2 \cdots p_k w_k \qquad (\text{with } p_i \in P, w_i \in \Gamma^*, k > 0)$ 

... an infinite state space

The transition relation of a DPN:

 $(p\gamma \xrightarrow{a} p_1 w_1) \in \Delta: \qquad u p \gamma v \xrightarrow{a} u p_1 w_1 v$  $(p\gamma \xrightarrow{a} p_1 w_1 \triangleright p_2 w_2) \in \Delta: \qquad u p \gamma v \xrightarrow{a} u p_2 w_2 p_1 w_1 v$ 

# Example

## Consider the following DPN with a single rule

 $p\gamma \xrightarrow{a} p\gamma\gamma \triangleright q\gamma$ 

Transitions:

ΡΥ *ϤΥΡΥΥ ϤΥϤΥΡΥΥΥ ϤΥϤΥϤΥΡΥΥΥΥ ϤΥϤΥϤΥΡΥΥΥΥ* 

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P induces trace language:  $L = \bigcup \{ A^n \cdot (B^m \otimes (C^i, D^j) \mid n \ge m \ge 0, i \ge j \ge 0 \}$ 

Cannot characterize L by constraint system with "·" and " $\otimes$ ". Trace languages of DPNs differ from those of PA processes. [Bouajjani, MO, Touili: CONCUR 2005]

## **Basic Results on Reachability Analysis of DPNs**

[Bouajjani, MO, Touili, CONCUR 2005]

Definition

 $\operatorname{pre}^{*}[L](C) := \{c \mid \exists d \in C, w \in L : c \xrightarrow{w} * d\}$  $\operatorname{post}^{*}[L](C) := \{d \mid \exists c \in C, w \in L : c \xrightarrow{w} * d\}$ 

Forward-Reachability

- 1) post\*[Act\*](C) is in general non-regular for regular C.
- 2) post\*[Act\*](C) is effectively context-free for context-free C (in polyn. time).
- 3) Membership in post\*[L](C) is in general undecidable for regular L.

### **Backward-Reachability**

- 1) pre<sup>\*</sup>[A<sup>\*</sup>](C) is effectively regular for regular C and A  $\subseteq$  Act (in polyn. time).
- 2) Membership in pre\*[L](C) is in general undecidable for regular L.

### Single Steps

 pre<sup>\*</sup>[A](C) and post<sup>\*</sup>[A](C) are effectively regular for regular C and A ⊆ Act (in polyn. time).

### **Example: Backward Reachability Analysis for DPNs**

Consider again DPN with the rule

 $p\gamma \xrightarrow{a} p\gamma\gamma \triangleright q\gamma$ 

and the infinite set of states

Bad = 
$$(q\gamma q\gamma p\gamma^{+})^{+} = L(A)$$

Analysis problem: can Bad be reached from  $p\gamma$ ?



# Some Applications of pre\*-Computations with unrestricted L (i.e. L = Act\*)

### Reachability of regular sets of configurations

Set Bad of configurations is reachable from initial configuration  $p_0\gamma_0$  iff

 $p_0\gamma_0 \in \text{ pre*}[\text{Act*}](\text{Bad})$ 

### Bounded model checking

used in JMoped of Schwoon/Esparza

By iterated pre\*-computations alternating with single steps corresponding to synchronizations/communications

Bit-vector data-flow analysis problems à la

à la [Esparza/Knoop, FOSSACS'99]

Variable x is live at program point u

iff

$$e_{Main} \in pre^{*}[Act^{*}](At_{u} \cap pre^{*}[NonDef_{x}^{*}](pre^{*}[Use_{x}](Conf)))$$

# **Exploiting a Tree-Shaped View of Configurations CDPNs: Constrained Dynamic Pushdown-Networks**

### Idea:

Add (regular, stable) pre-conditions over current control symbols of children threads to DPN rules.

A constrained dynamic pushdown-network (CDPN) consists of:

- P, a finite set of control symbols
- Γ, a finite set of stack symbols
- $\Delta$ , a finite set of rules of the following form

 $\phi: p\gamma \xrightarrow{a} p_1 w_1 \qquad \text{where } \phi \subseteq P^*$  $\phi: p\gamma \xrightarrow{a} p_1 w_1 \triangleright p_2 w_2 \qquad \text{where } \phi \subseteq P^*$  $(\text{with } p, p_1, p_2 \in \mathsf{P}, \gamma \in \Gamma, w_1, w_2 \in \Gamma^*, a \in \mathsf{Act})$ 

# **Example: A CDPN**

1. Phase: 
$$p\gamma \xrightarrow{a} p\gamma\gamma \triangleright q_0\gamma$$
  
 $\phi: p\gamma \xrightarrow{b} p'$  with  $\phi = ((q_1 + q_2)q_2)^*$   
2. Phase:  $p'\gamma \xrightarrow{c} p'$ 

$$q_0 \gamma \xrightarrow{d} q_1 \gamma$$
$$q_1 \gamma \xrightarrow{e} q_2 \gamma$$

Constraint  $\phi$  means: Proceed to second phase only if:

- an even number of children threads has been created,
- each second child has terminated, and
- each child has performed at least one step.



# **Reachability Analysis of CDPNs**

### Definition

Constraint  $\phi$  is called stable for  $\Delta$  if:

 $upv \in \phi$ ,  $(\psi: p\gamma \xrightarrow{a} p_1 w_1) \in \Delta$  implies  $up_1 v \in \phi$ , and

 $upv \in \phi$ ,  $(\psi: p\gamma \xrightarrow{a} p_1w_1 \triangleright p_2w_2) \in \Delta$  implies  $up_1v \in \phi$ 

Theorem for CDPNs [Bouajjani, MO, Touili, CONCUR 2005]

pre\*[Act\*](C) is effectively regular for regular C and A  $\subseteq$  Act, if all constraints  $\phi$  occuring in rules of the CDPN are regular and stable for  $\Delta$ .

Problem at least PSPACE-hard

### Modelling power of stable constraints:

Parallel procedure calls, various join-statements, return values from parallel procedure calls, phased execution.

## Modelling Power of Stable Regular Constraints

As a preparation: Indicate termination of son threads by a special control state §:

for spawn edge e: spawn P

$$g\left\langle l,u\right\rangle \xrightarrow{e} g\left\langle l,v\right\rangle \rhd g_{\text{init}}\left\langle l_{\text{init}},e_{P}\right\rangle$$

one special type of rules:

$$p$$
\$ $\xrightarrow{e}$ \$

Model parallel call to two procedures:

for parallel call edge e:  

$$\begin{array}{c}
u \\
pcall(P,Q) \\
v\end{array}
\qquad g \langle l,u \rangle \xrightarrow{PIL} g \langle l,u^1 \rangle \triangleright g_{init} \langle l_{init},e_P \rangle \$ \\
g \langle l,u^1 \rangle \xrightarrow{IIQ} g \langle l,u^2 \rangle \triangleright g_{init} \langle l_{init},e_Q \rangle \$ \\
P^*\$\$:g \langle l,u^2 \rangle \xrightarrow{PIQ} g \langle l,v \rangle
\end{array}$$

**}** 

# Modelling Power of Stable Regular Constraints (Ctd.)

Model various types of join-statements:

- proceed if all children have terminated: §\*: ...
- proceed if last child has terminated:
- proceed if some child has terminated: P\*\$P\*: ...
- proceed if every second child has terminated:  $(P \S)^*(P + \varepsilon)$ : ...
- ...

Model return values of parallel procedures (beyond PA!):

$$P^* \$_p \$_q : g \left\langle l, u^2 \right\rangle \xrightarrow{P \parallel Q} g_{pq} \left\langle l, v \right\rangle$$

P\*§: ...

Model phased execution

# **Synchronization via Locks**

- Assume finite set of locks
- Have acquire- and release actions
  - $acq L, rel L \in Act$  f.a. locks L
- Intuition: At any time a lock can be hold by at most one thread
- Goal of lock-sensitive analysis

# The Results of Kahlon and Gupta

### Theorem 1 [Kahlon/Gupta, LICS 2006]

Reachability is undecidable for two pushdown-systems running in parallel and synchronizing by release- and acquire-operations used in an unstructured way.

Idea: Can simulate synchronous communication

### Theorem 2 [Kahlon/Gupta, LICS 2006]

Reachability is decidable for two pushdown-systems running in parallel and synchronizing by release- and acquire-operations used in a nested fashion.

Idea: Collect information about lock usage of each process in **"acquisition histories**" and check mutual consistency of the collected histories.

Our goal: Lock-sensitive analysis for systems with thread creation

# **Example: Locksets are not Precise Enough**

Thread 1:	Thread 2:
acquire L1	acquire L2;
acquire L2	acquire L1;
release L2	release L1;
X:	Y:

Must-Lockset computed at X: { L1 } Must-Lockset computed at Y: { L2 }

We have disjoint locksets at X and Y: { L1 }  $\cap$  { L2 } = { }.

Nevertheless, X and Y are not reachable simultaneously !

### **A Tree-Based View of Executions: Action Trees**

A DPN:  $p\gamma \xrightarrow{sp} p\gamma \triangleright q_0\gamma$   $q_0\gamma \xrightarrow{d} q_1\gamma$  $q_1\gamma \xrightarrow{e} q_2\gamma$ 



### **A Tree-Based View of Executions**

Definition

$$\operatorname{pre}^{*}[L](C) := \{c \mid \exists d \in C, w \in L : c \xrightarrow{w} * d\} \quad \text{where } L \subseteq Act *$$
$$\operatorname{preT}^{*}[M](C) := \{c \mid \exists d \in C, T \in M : c \xrightarrow{T} * d\} \quad \text{where } M \subseteq Trees(Act)$$

Recall:

Membership in pre\*[L](C) is undecidable for regular L already for very simple languages C (e.g. singletons).

#### Theorem for DPNs [Lammich, MO, Wenner, CAV 2009]

preT\*[M](C) is effectively regular for regular C and regular M (on trees).

#### Theorem 2 [Lammich, MO, Wenner, CAV 2009]

In a DPN that uses locks in a well-nested and non-reentrant fashion: Set of tree-shaped executions having a lock-sensitive schedule is regular.

Idea of proof: Generalize Kahlon and Gupta's acquisition histories.

Size of automaton exponential in number of locks...



# **Applications**

### Lock-(join-)sensitive ...

- ... reachability analysis to regular sets of configurations
- ... bounded model checking
- ... DFA of bitvector problems



## More Recent Work (VMCAI 2011): An Even More Regular View to Executions: Execution Trees

Joint work with:

- Thomas Gawlitza, Helmut Seidl (TU München)
- Peter Lammich, Alexander Wenner (WWU Münster)

Realised for Java analysis: Benedikt Nordhoff's diploma thesis

### Example:

 $\begin{aligned} Call_{0} &: \quad p\gamma \xrightarrow{cl} p'\gamma\gamma & Ret_{4} &: \quad q\gamma \xrightarrow{ret_{4}} q \\ Spawn_{1} &: \quad p'\gamma \xrightarrow{sp} p\gamma \triangleright q\gamma \\ Ret_{2} &: \quad p\gamma \xrightarrow{ret_{2}} p'' \\ Ret_{3} &: \quad p''\gamma \xrightarrow{ret_{3}} p'' \end{aligned}$ 



# **Execution Trees**

**Recall:** post\*[Act\*]( $p_0\gamma_0$ ) is non-regular in general.

### Observation 1:

Set of all execution trees from given initial config., postE\*( $p_0\gamma_0$ ), is regular !

### **Observation 2:**

Set of execution trees that have a lock-sensitive schedule is regular, e.g. for:

- · nested non-reentrant locking with structured form of joins
- reentrant block-structured locking (monitors, synchronized-blocks)

### **Observation 3:**

Set of execution trees reaching a given regular set C of configs is regular

### Obtain homogenous approach to, e.g., lock-sensitive reachability:

Reg. set C is lock-sensitively reachable from start config  $p_0\gamma_0$  iff

 $postE^*(p_0\gamma_0) \cap LockSensTrees \cap ExecTrees(C)$  is non-empty.

# (Finite) Tree-Automata

#### Definition

Let  $\Sigma$  be a finite ranked alphabet.

#### (Finite bottom-up) tree automaton (over $\Sigma$ ):

A structure  $T = (Q, Q_F, \delta)$  with:

- · Q: finite set of states
- $Q_F \subseteq Q$ : accepting states
- $\delta$ : set of rules of the form:  $f(q_1,...,q_k) \rightarrow q$  with  $q,q_1,...,q_k \in Q$ ,  $f \in \Sigma$  of rank  $k \ge 0$

#### Acceptance:

a) If

- T accepts trees  $t_1, \dots, t_k$  in states  $q_1, \dots, q_k$  and
- + T has rule  $f(q_1,...,q_k) \rightarrow q$  then
  - T accepts tree  $f(t_1,...,t_k)$  in state q
- b) T accepts a tree t

if T accepts t in an accepting state  $q \in Q_F$ 



# **Example: (Finite) Tree-Automaton**

#### Ranked alphabet Σ:

Rank 0: true, false	Rank 1: not
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#### Tree automaton:

 $T=(\;\{\perp,\top\},\,\{\top\},\,\delta\;)\;$  with

- $\delta: \text{ true } \rightarrow \top \quad \text{not}(\bot) \rightarrow \top \quad \text{or}(\bot,\bot) \rightarrow \bot$   $false \rightarrow \bot \quad \text{not}(\top) \rightarrow \bot \quad \text{or}(\bot,\bot) \rightarrow \top$ 
  - false  $\rightarrow \bot$  not $(\top) \rightarrow \bot$  or $(\bot, \top) \rightarrow \top$



Rank 2: and, or

and( $\perp, \perp$ ) $\rightarrow \perp$
and( $\perp, \top$ ) $\rightarrow \perp$
and( $\top, \perp$ ) $\rightarrow \perp$
and $(\top,\top) \rightarrow \top$

#### Acceptance of example tree:

not ( and ( or (true, false), false ))



### **Tree Automaton for Execution Trees of a DPN**



b) c = N and T represents non-terminating executions from  $p\gamma$ 

### Rules:

Nil:  $[nil_{p\gamma}] \rightarrow (p, \gamma, N)$ Base rules:  $[p\gamma \xrightarrow{a} p'\gamma']((p', \gamma', c)) \rightarrow (p, \gamma, c)$ Call rules:  $[p\gamma \xrightarrow{X} p'\gamma'\gamma'']((p', \gamma', p''), (p'', \gamma'', c)) \rightarrow (p, \gamma, c)$   $[p\gamma \xrightarrow{X} p'\gamma'\gamma'']((p', \gamma', N)) \rightarrow (p, \gamma, N)$ Return rules:  $[p\gamma \xrightarrow{a} p'] \rightarrow (p, \gamma, p')$ Spawn rules:  $[p\gamma \xrightarrow{a} p'\gamma' \triangleright p''\gamma'']((p', \gamma', c), (p'', \gamma'', _)) \rightarrow (p, \gamma, c)$ 

### Tree Automaton for Execution Trees with Lock-Sensitive Schedule

**States:** (G, A, U) with  $A, U \subseteq Locks, G \subseteq Locks \times Locks$ , accepting if G is acyclic

Idea: 
$$(G, A, U)$$
 accepts tree T

iff

- a) no lock is finally acquired more than once in T,
- b) G contains edge  $x \rightarrow y$  if lock y is used in T after lock x has been finally acquired,
- c) A is the set of finally acquired locks, and
- d) U is the set of used locks.

Rules: Nil: $[nil_{p\gamma}] \rightarrow (\emptyset, \emptyset, \emptyset)$ Base rules: $[p\gamma \xrightarrow{a} p'\gamma']((G, A, U)) \rightarrow (G, A, U)$ Call rules: $[p\gamma \xrightarrow{X} p'\gamma'\gamma'']((G, A, U), (G', A', U')) \rightarrow$ if  $A \cap A' = \emptyset$  $[p\gamma \xrightarrow{X} p'\gamma'\gamma'']((G, A, U)) \rightarrow (G \cup X \times A, A \cup X, U)$ if  $A \cap X = \emptyset$ Return rules: $[p\gamma \xrightarrow{a} p'] \rightarrow (\emptyset, \emptyset, \emptyset)$ Spawn rules: $[p\gamma \xrightarrow{a} p'\gamma' \triangleright p''\gamma'']((G, A, U), (G', A', U')) \rightarrow (G \cup G', A \cup A', U \cup U')$ if  $A \cap A' = \emptyset$ 

# **Realization for Java**

Diploma thesis of Benedikt Nordhoff

Uses:

- WALA from IBM: T.J. Watson Libraries for Analysis
- XSB: A Prolog-like system with tabulating evaluation

Identifies object references that can be used as locks

For practicality:

- Pre-analysis of WALA flow graph and (massive) pruning
- Modular reformulation of automata-based analysis
- Clever evaluation strategy for tree automata construction

Experimental applications:

- Monitor-sensitive data-race analyzer for Java
- RS3 context: Improve PDG-based IFC analysis of concurrent Java







# Conclusion

- Lock-join-sensitive analysis using automata
- Finite state + recursion + thread creation + locks + joins
- Experimental applications for Java
- Trees are better than words
- Keeping more structure in the trees is even better